Test Booklet Code
G

Time : 3 hrs.

# Answers \& Solutions 

M.M. : 360
for

## JEE (MAIN)-2014

(Mathematics, Physics \& Chemistry)

## Important Instructions:

1. The test is of $\mathbf{3}$ hours duration.
2. The Test Booklet consists of $\mathbf{9 0}$ questions. The maximum marks are $\mathbf{3 6 0}$.
3. There are three parts in the question paper A, B, C consisting of Mathematics, Physics and Chemistry having 30 questions in each part of equal weightage. Each question is allotted 4 (four) marks for each correct response.
4. Candidates will be awarded marks as stated above in Instructions No. 3 for correct response of each question. $1 / 4$ (one-fourth) marks will be deducted for indicating incorrect response of each question. No deduction from the total score will be made if no response is indicated for an item in the answer sheet.
5. There is only one correct response for each question. Filling up more than one response in each question will be treated as wrong response and marks for wrong response will be deducted accordingly as per instruction 4 above.
6. Use Blue/Black Ball Point Pen only for writing particulars/marking responses on Side-1 and Side-2 of the Answer Sheet. Use of pencil is strictly prohibited.
7. No candidate is allowed to carry any textual material, printed or written, bits of papers, pager, mobile phone, any electronic device, etc. except the Admit Card inside the examination hall/room.
8. The CODE for this Booklet is G. Make sure that the CODE printed on Side-2 of the Answer Sheet is the same as that on this booklet. In case of discrepancy, the candidate should immediately report the matter to the Invigilator for replacement of both the Test Booklet and the Answer Sheet.

## PART-A : MATHEMATICS

1. If $x=-1$ and $x=2$ are extreme points of $f(x)=\alpha \log |x|+\beta x^{2}+x$ then
(1) $\alpha=-6, \beta=-\frac{1}{2}$
(2) $\alpha=2, \beta=-\frac{1}{2}$
(3) $\alpha=2, \beta=\frac{1}{2}$
(4) $\alpha=-6, \beta=\frac{1}{2}$

Answer (2)
Sol. $f(x)=\alpha \log |x|+\beta x^{2}+x$
$f^{\prime}(x)=\frac{\alpha}{x}+2 \beta x+1=0$ at $x=-1,2$
$-\alpha-2 \beta+1=0 \Rightarrow \alpha+2 \beta=1$
$\frac{\alpha}{2}+4 \beta+1=0 \Rightarrow \alpha+8 \beta=-2$
$6 \beta=-3 \Rightarrow \beta=-\frac{1}{2}$
$\therefore \alpha=2$
2. The locus of the foot of perpendicular drawn from the centre of the ellipse $x^{2}+3 y^{2}=6$ on any tangent to it is
(1) $\left(x^{2}-y^{2}\right)^{2}=6 x^{2}-2 y^{2}$
(2) $\left(x^{2}+y^{2}\right)^{2}=6 x^{2}+2 y^{2}$
(3) $\left(x^{2}+y^{2}\right)^{2}=6 x^{2}-2 y^{2}$
(4) $\left(x^{2}-y^{2}\right)^{2}=6 x^{2}+2 y^{2}$

Answer (2)
Sol. Here ellipse is $\frac{x^{2}}{a^{2}}+\frac{y^{2}}{b^{2}}=1$, where $a^{2}=6, b^{2}=2$
Now, equation of any variable tangent is

$$
\begin{equation*}
y=m x \pm \sqrt{a^{2} m^{2}+b^{2}} \tag{i}
\end{equation*}
$$

where $m$ is slope of the tangent
So, equation of perpendicular line drawn from centre to tangent is

$$
\begin{equation*}
y=\frac{-x}{m} \tag{ii}
\end{equation*}
$$

Eliminating $m$, we get
$\left(x^{2}+y^{2}\right)^{2}=a^{2} x^{2}+b^{2} y^{2}$
$\Rightarrow \quad\left(x^{2}+y^{2}\right)^{2}=6 x^{2}+2 y^{2}$
3. Let $f_{k}(x)=\frac{1}{k}\left(\sin ^{k} x+\cos ^{k} x\right)$ where $x \in R$ and $k \geq 1$. Then $f_{4}(x)-f_{6}(x)$ equals
(1) $\frac{1}{3}$
(2) $\frac{1}{4}$
(3) $\frac{1}{12}$
(4) $\frac{1}{6}$

## Answer (3)

Sol. $f_{k}(x)=\frac{1}{k}\left(\sin ^{k} x+\cos ^{k} x\right)$

$$
\begin{aligned}
& f_{4}(x)-f_{6}(x)=\frac{1}{4}\left(\sin ^{4} x+\cos ^{4} x\right)-\frac{1}{6}\left(\sin ^{6} x+\cos ^{6} x\right) \\
& =\frac{1}{4}\left[1-2 \sin ^{2} x \cos ^{2} x\right]-\frac{1}{6}\left[1-3 \sin ^{2} x \cos ^{2} x\right] \\
& =\frac{1}{4}-\frac{1}{6}=\frac{1}{12}
\end{aligned}
$$

4. If $X=\left\{4^{n}-3 n-1: n \in N\right\}$ and $Y=\{9(n-1): n \in N\}$, where $N$ is the set of natural numbers, then $X \cup Y$ is equal to
(1) $Y-X$
(2) $X$
(3) $Y$
(4) $N$

## Answer (3)

Sol. $X=\left\{(1+3)^{n}-3 n-1, n \in N\right\}$
$\left.=3^{2}\left(\begin{array}{lllll} \\ { }^{n} C_{2} & { }^{n} C_{3} \cdot 3 & \ldots & 3^{n}\end{array}\right), n \quad N\right\}$
$=\{$ Divisible by 9$\}$
$Y=\{9(n-1), n \in N\}$

$$
=(\text { All multiples of } 9\}
$$

So, $X \subseteq Y$
i.e., $X \cup Y=Y$
5. If $A$ is an $3 \times 3$ non-singular matrix such that $A A^{\prime}=A^{\prime} A$ and $B=A^{-1} A^{\prime}$, then $B B^{\prime}$ equals
(1) $I$
(2) $B^{-1}$
(3) $\left(B^{-1}\right)^{\prime}$
(4) $I+B$

Answer (1)

Sol. $B B^{\prime}=\left(A^{-1} . A^{\prime}\right)\left(A\left(A^{-1}\right)^{\prime}\right)$

$$
\begin{aligned}
& =A^{-1} \cdot A \cdot A^{\prime} \cdot\left(A^{-1}\right)^{1} \quad\left\{\text { as } A A^{\prime}=A^{\prime} A\right\} \\
& =I\left(A^{-1} A\right)^{\prime} \\
& =I \cdot I=I^{2}=I
\end{aligned}
$$

6. The integral $\int\left(1+x-\frac{1}{x}\right) e^{x+\frac{1}{x}} d x$ is equal to
(1) $x e^{x+\frac{1}{x}}+c$
(2) $(x+1) e^{x+\frac{1}{x}}+c$
(3) $-x e^{x+\frac{1}{x}}+c$
(4) $(x-1) e^{x+\frac{1}{x}}+c$

## Answer (1)

Sol. $I=\int\left\{e^{\left(x+\frac{1}{x}\right)}+x\left(1-\frac{1}{x^{2}}\right) e^{x+\frac{1}{x}}\right\} d x$ $=x \cdot e^{x \frac{1}{x}} c$

As $\quad\left(x f^{\prime}(x) \quad f(x)\right) d x \quad x f(x) \quad$ c
7. The area of the region described by $A=\left\{(x, y): x^{2}+y^{2} \leq 1\right.$ and $\left.y^{2} \leq 1-x\right\}$ is
(1) $\frac{\pi}{2}-\frac{4}{3}$
(2) $\frac{\pi}{2}-\frac{2}{3}$
(3) $\frac{\pi}{2}+\frac{2}{3}$
(4) $\frac{\pi}{2}+\frac{4}{3}$

## Answer (4)

Sol.


Shaded area

$$
\begin{aligned}
& \frac{(1)^{2}}{2} 2_{0}^{1} \sqrt{(1 \quad x)} d x \\
& \left.\overline{2} \frac{2(1 \quad x)^{3 / 2}}{3 / 2}(1)\right|_{0} ^{1} \\
& \overline{2} \frac{4}{3}(0 \quad(1)) \\
& \overline{2} \frac{4}{3}
\end{aligned}
$$

8. The image of the line
$\frac{x-1}{3}=\frac{y-3}{1}=\frac{z-4}{-5}$ in the plane $2 x-y+z+3=0$ is the line
(1) $\frac{x+3}{-3}=\frac{y-5}{-1}=\frac{z+2}{5}$
(2) $\frac{x-3}{3}=\frac{y+5}{1}=\frac{z-2}{-5}$
(3) $\frac{x-3}{-3}=\frac{y+5}{-1}=\frac{z-2}{5}$
(4) $\frac{x+3}{3}=\frac{y-5}{1}=\frac{z-2}{-5}$

## Answer (4)

Sol.


$$
\frac{a 1}{2} \quad \frac{b-3}{1} \frac{c 4}{1}
$$

$$
\Rightarrow \quad a=2 \lambda+1
$$

$$
b=3-\lambda
$$

$$
c=4+\lambda
$$

$P \quad 1,3 \quad \overline{2}, 4 \quad \overline{2}$

2( 1) $3 \quad \overline{2} \quad 4 \quad \overline{2} \quad 3 \quad 0$
$2 \quad 2 \quad 3+\frac{1}{2} 4 \underset{2}{ } 30$
$3 \lambda+6=0 \Rightarrow \lambda=-2$
$a=-3, b=5, c=2$
So the equation of the required line is
$\begin{array}{llll}x \quad 3 & y \quad 5 & z \quad 2 \\ 5\end{array}$
9. The variance of first 50 even natural numbers is
(1) 833
(2) 437
(3) $\frac{437}{4}$
(4) $\frac{833}{4}$

Answer (1)

Sol. Variance $=\frac{\Sigma x_{i}^{2}}{N}-(\bar{x})^{2}$

$$
\begin{aligned}
\Rightarrow \quad \sigma^{2} & =\frac{2^{2}+4^{2}+\ldots+100^{2}}{50}-\left(\frac{2+4+\ldots+100}{50}\right)^{2} \\
& =\frac{4\left(1^{2}+2^{2}+3^{2}+\ldots .+50^{2}\right)}{50}-(51)^{2} \\
& =4\left(\frac{50 \times 51 \times 101}{50 \times 6}\right)-(51)^{2} \\
& =3434-2601 \\
\Rightarrow \sigma^{2} & =833
\end{aligned}
$$

10. If $z$ is a complex number such that $|z| \geq 2$, then the minimum value of $\left|z+\frac{1}{2}\right|$
(1) Lies in the interval $(1,2)$
(2) Is strictly greater than $\frac{5}{2}$
(3) Is strictly greater than $\frac{3}{2}$ but less than $\frac{5}{2}$
(4) Is equal to $\frac{5}{2}$

## Answer (1)

Sol.

$\left|z+\frac{1}{2}\right|$
So, $\left||z|-\frac{1}{2}\right| \leq\left|z+\frac{1}{2}\right|$
$\Rightarrow\left|z+\frac{1}{2}\right| \geq\left|2-\frac{1}{2}\right|$
$\Rightarrow\left|z+\frac{1}{2}\right| \geq \frac{3}{2}$
11. Three positive numbers form an increasing G.P. If the middle term in this G.P. is doubled, the new numbers are in A.P. Then the common ratio of the G.P. is
(1) $3+\sqrt{2}$
(2) $2-\sqrt{3}$
(3) $2+\sqrt{3}$
(4) $\sqrt{2}+\sqrt{3}$

Answer (3)
Sol. $a, a r, a r^{2} \rightarrow$ G.P.
$a, 2 a r, a r^{2} \rightarrow$ A.P.
$2 \times 2 a r=a+a r^{2}$
$4 r=1+r^{2}$
$\Rightarrow r^{2}-4 r+1=0$

$$
r=\frac{4 \pm \sqrt{16-4}}{2}=2 \pm \sqrt{3}
$$

$$
r=2+\sqrt{3}
$$

$r=2-\sqrt{3}$ is rejected
$\because(r>1)$
G.P. is increasing.
12. If the coefficients of $x^{3}$ and $x^{4}$ in the expansion of $\left(1+a x+b x^{2}\right)(1-2 x)^{18}$ in powers of $x$ are both zero, then $(a, b)$ is equal to
(1) $\left(14, \frac{251}{3}\right)$
(2) $\left(14, \frac{272}{3}\right)$
(3) $\left(16, \frac{272}{3}\right)$
(4) $\left(16, \frac{251}{3}\right)$

## Answer (3)

Sol. $\left(1+a x+b x^{2}\right)(1-2 x)^{18}$

$$
\begin{aligned}
& \left(1+a x+b x^{2}\right)\left[{ }^{18} C_{0}-{ }^{18} C_{1}(2 x)+{ }^{18} C_{2}(2 x)^{2}-\right. \\
& \left.{ }^{18} C_{3}(2 x)^{3}+{ }^{18} C_{4}(2 x)^{4}-\ldots . . . .\right]
\end{aligned}
$$

Coeff. of $x^{3}=-{ }^{18} C_{3} .8+a \times 4 .{ }^{18} C_{2}-2 b \times 18=0$

$$
\begin{align*}
& =-\frac{18 \times 17 \times 16}{6} .8+\frac{4 a+18 \times 17}{2}-36 b=0 \\
& =-51 \times 16 \times 8+a \times 36 \times 17-36 b=0 \\
& =-34 \times 16+51 a-3 b=0 \\
& =51 a-3 b=34 \times 16=544 \\
& =51 a-3 b=544 \tag{i}
\end{align*}
$$

Only option number (3) satisfies the equation number (i).
13. Let $a, b, c$ and $d$ be non-zero numbers. If the point of intersection of the lines $4 a x+2 a y+c=0$ and $5 b x+2 b y+d=0$ lies in the fourth quadrant and is equidistant from the two axes then
(1) $2 b c+3 a d=0$
(2) $3 b c-2 a d=0$
(3) $3 b c+2 a d=0$
(4) $2 b c-3 a d=0$

Answer (2)
Sol. Let $(\alpha,-\alpha)$ be the point of intersection
$\therefore 4 \mathrm{a} \alpha-2 \mathrm{a} \alpha+\mathrm{c}=0 \quad \frac{c}{2 a}$
and $5 b \alpha-2 b \alpha+d=0$
$\frac{d}{3 b}$

$$
\begin{aligned}
& 3 b c=2 a d \\
& 3 b c-2 a d=0
\end{aligned}
$$

## Alternative method :

The point of intersection will be

$$
\begin{aligned}
& \frac{x}{2 a d-2 b c}=\frac{-y}{4 a d-5 b c}=\frac{1}{8 a b-10 a b} \\
\Rightarrow & x=\frac{2(a d-b c)}{-2 a b} \\
\Rightarrow & y=\frac{5 b c-4 a d}{-2 a b}
\end{aligned}
$$

$\because \quad$ Point of intersection is in fourth quadrant so $x$ is positive and $y$ is negative.
Also distance from axes is same
So $x=-y(\because$ distance from $x$-axis is $-y$ as $y$ is negative)

$\frac{2(a d-b c)}{-2 a b}=\frac{-(5 b c-4 a d)}{-2 a b}$
$2 a d-2 b c=-5 b c+4 a d$
$\Rightarrow 3 b c-2 a d=0$
14. If $[\vec{a} \times \vec{b} \vec{b} \times \vec{c} \vec{c} \times \vec{a}]=\lambda[\vec{a} \vec{b} \vec{c}]^{2}$ then $\lambda$ is equal to
(1) 3
(2) 0
(3) 1
(4) 2

Answer (3)

Sol. L.H.S.
$=(\bar{a} \times \bar{b}) \cdot[(\vec{b} \times \vec{c}) \times(\vec{c} \times \vec{a})]$
$=(\vec{a} \times \vec{b}) \cdot[(\vec{b} \times \vec{c} \cdot \vec{a}) \vec{c}-(\vec{b} \times \vec{c} \cdot \vec{c}) \vec{a}]$
$=(\vec{a} \times \vec{b}) \cdot[[\bar{b} \bar{c} \bar{a}] \vec{c}] \quad[\because \vec{b} \times \vec{c} \cdot \vec{c}=0]$
$=[\bar{a} \bar{b} \bar{c}] \cdot(\bar{a} \times \bar{b} \cdot \bar{c})=[\bar{a} \bar{b} \bar{c}]^{2}$
$\left[\begin{array}{lll}\vec{a} \times \vec{b} & \vec{b} \times \vec{c} & \vec{c} \times \vec{a}\end{array}\right]=\left[\begin{array}{ll}\bar{a} \bar{b} \bar{c}\end{array}\right]^{2}$
So $\lambda=1$
15. Let $A$ and $B$ be two events such that $P(\overline{A \cup B})=\frac{1}{6}, P(A \cap B)=\frac{1}{4}$ and $P(\bar{A})=\frac{1}{4}$, where $\bar{A}$ stands for the complement of the event $A$. Then the events $A$ and $B$ are
(1) Equally likely but not independent
(2) Independent but not equally likely
(3) Independent and equally likely
(4) Mutually exclusive and independent

## Answer (2)

Sol. $P(\overline{A \cup B})=\frac{1}{6} \Rightarrow P(A \cup B)=1-\frac{1}{6}=\frac{5}{6}$
$P(\bar{A})=\frac{1}{4} \Rightarrow P(A)=1-\frac{1}{4}=\frac{3}{4}$
$\because P(A \cup B)=P(A)+P(B)-P(A \cap B)$
$\frac{5}{6}=\frac{3}{4}+P(B)-\frac{1}{4}$
$P(B)=\frac{1}{3}$
$\because \quad P(A) \neq P(B)$ so they are not equally likely.
Also $P(A) \times P(B)=\frac{3}{4} \times \frac{1}{3}=\frac{1}{4}$
$=P(A \cap B)$
$\because \quad P(A \cap B)=P(A) \cdot P(B)$ so $A \& B$ are independent.
16. Let $P S$ be the median of the triangle with vertices $P(2,2), Q(6,-1)$ and $R(7,3)$. The equation of the line passing through $(1,-1)$ and parallel to $P S$ is
(1) $2 x+9 y+7=0$
(2) $4 x+7 y+3=0$
(3) $2 x-9 y-11=0$
(4) $4 x-7 y-11=0$

Answer (1)

Sol.

$S$ is mid-point of $Q R$
So $S=\left(\frac{7+6}{2}, \frac{3-1}{2}\right)$

$$
=\left(\frac{13}{2}, 1\right)
$$

Slope of $P S=\frac{2-1}{2-\frac{13}{2}}=-\frac{2}{9}$
Equation of line $\Rightarrow y-(-1)=-\frac{2}{9}(x-1)$
$9 y+9=-2 x+2 \Rightarrow 2 x+9 y+7=0$
17. $\lim _{x \rightarrow 0} \frac{\sin \left(\pi \cos ^{2} x\right)}{x^{2}}$ is equal to
(1) 1
(2) $-\pi$
(3) $\pi$
(4) $\frac{\pi}{2}$

Answer (3)
Sol. $\lim _{x \rightarrow 0} \frac{\sin \left(\pi \cos ^{2} x\right)}{x^{2}}$
$=\lim _{x \rightarrow 0} \frac{\sin \left(\pi\left(1-\sin ^{2} x\right)\right.}{x^{2}}$
$=\lim _{x \rightarrow 0} \sin \frac{\left(\pi-\pi \sin ^{2} x\right)}{x^{2}}$
$=\lim _{x \rightarrow 0} \sin \frac{\left(\pi \sin ^{2} x\right)}{x^{2}} \quad[\because \sin (\pi-\theta)=\sin \theta]$
$=\lim _{x \rightarrow 0} \sin \frac{\left(\pi \sin ^{2} x\right)}{\left(\pi \sin ^{2} x\right)} \times \frac{\pi \sin ^{2} x}{x^{2}}$
$=\lim _{x \rightarrow 0} 1 \times \pi\left(\frac{\sin x}{x}\right)^{2}=\pi$
18. Let $\alpha$ and $\beta$ be the roots of equation $p x^{2}+q x+r=0, p \neq 0$. If $p, q, r$ are in A.P. and $\frac{1}{\alpha}+\frac{1}{\beta}=4$, then the value of $|\alpha-\beta|$ is
(1) $\frac{2 \sqrt{17}}{9}$
(2) $\frac{\sqrt{34}}{9}$
(3) $\frac{2 \sqrt{13}}{9}$
(4) $\frac{\sqrt{61}}{9}$

## Answer (3)

Sol.
$\because p, q, r$ are in $A P$
$2 q=p+r$
Also $\frac{1}{\alpha}+\frac{1}{\beta}=4$
$\Rightarrow \frac{\alpha+\beta}{\alpha \beta}=4$
$=\frac{-\frac{q}{p}}{\frac{r}{p}}=4 \Rightarrow q=-4 r$
From (i)
$2(-4 r)=p+r$
$p=-9 r$
$q=-4 r$
$r=r$
Now $|\alpha-\beta|=\sqrt{(\alpha+\beta)^{2}-4 \alpha \beta}$
$=\sqrt{\left(\frac{-q}{p}\right)^{2}-\frac{4 r}{p}}$
$=\frac{\sqrt{q^{2}-4 p r}}{|p|}$
$=\frac{\sqrt{16 r^{2}+36 r^{2}}}{|-9 r|}$
$=\frac{2 \sqrt{13}}{9}$
19. A bird is sitting on the top of a vertical pole 20 m high and its elevation from a point $O$ on the ground is $45^{\circ}$. It flies off horizontally straight away from the point $O$. After one second, the elevation of the bird from $O$ is reduced to $30^{\circ}$. Then the speed (in $\mathrm{m} / \mathrm{s}$ ) of the bird is
(1) $40(\sqrt{3}-\sqrt{2})$
(2) $20 \sqrt{2}$
(3) $20(\sqrt{3}-1)$
(4) $40(\sqrt{2}-1)$

## Answer (3)

Sol.

$t=1 \mathrm{~s}$
From figure $\tan 45^{\circ}=\frac{20}{x}$
and $\tan 30^{\circ}=\frac{20}{x+y}$
so, $y=20(\sqrt{3}-1)$
i.e., speed $=20(\sqrt{3}-1) \mathrm{m} / \mathrm{s}$.
20. If $a \in R$ and the equation
$-3(x-[x])^{2}+2(x-[x])+a^{2}=0$
(where $[x]$ denotes the greatest integer $\leq x$ ) has no integral solution, then all possible values of $a$ lie in the interval
(1) $(1,2)$
(2) $(-2,-1)$
(3) $(-\infty,-2) \cup(2, \infty)$
(4) $(-1,0) \cup(0,1)$

Answer (4)
Sol. $-3(x-[x])^{2}+2[x-[x])+a^{2}=0$
$3\{x\}^{2}-2\{x\}-a^{2}=0$
$a \neq 0,3\left(\{x\}^{2}-\frac{2}{3}\{x\}\right)=a^{2}$
$a^{2}=3\left(\{x\}-\frac{1}{3}\right)^{2}-\frac{1}{3}$
$0 \leq\{x\}<1$ and $-\frac{1}{3} \leq\{x\}-\frac{1}{3}<\frac{2}{3}$
$\begin{array}{lllll}0 & 3 & \{x\} & \frac{1}{3}^{2} & \frac{4}{3}\end{array}$
$\begin{array}{lllll}\frac{1}{3} & 3 & \{x\} & \frac{1}{3}^{2} & \frac{1}{3} \\ 1\end{array}$
For non-integral solution
$0<a^{2}<1$ and $a \in(-1,0) \cup(0,1)$

## Alternative

$-3\{x\}^{2}+2\{x\}+a^{2}=0$
Now, $-3\{x\}^{2}+2\{x\}$

to have no integral roots $0<a^{2}<1$
$\therefore \quad a \in(-1,0) \cup(0,1)$
21. The integral
$\int_{0}^{\pi} \sqrt{1+4 \sin ^{2} \frac{x}{2}-4 \sin \frac{x}{2}} d x$ equals
(1) $\frac{2 \pi}{3}-4-4 \sqrt{3}$
(2) $4 \sqrt{3}-4$
(3) $4 \sqrt{3}-4-\frac{\pi}{3}$
(4) $\pi-4$

Answer (3)
Sol. $\int_{0}^{\pi} \sqrt{1+4 \sin ^{2} \frac{x}{2}-4 \sin \frac{x}{2}} d x$

$$
=\int_{0}^{\pi}\left|2 \sin \frac{x}{2}-1\right| d x \quad\left[\begin{array}{l}
\sin \frac{x}{2}=\frac{1}{2} \\
\Rightarrow \frac{x}{2}=\frac{\pi}{6} \rightarrow x=\frac{\pi}{3} \\
\frac{x}{2}=\frac{5 \pi}{6} \rightarrow x=\frac{5 \pi}{3}
\end{array}\right]
$$

$=\int_{0}^{\pi / 3}\left(1-2 \sin \frac{x}{2}\right) d x+\int_{\pi / 3}^{\pi}\left(2 \sin \frac{x}{2}-1\right) d x$
$=\left[x+4 \cos \frac{x}{2}\right]_{0}^{\pi / 3}+\left[-4 \cos \frac{x}{2}-x\right]_{\pi / 3}^{\pi}$
$=\frac{\pi}{3}+4 \frac{\sqrt{3}}{2}-4+\left(0-\pi+4 \frac{\sqrt{3}}{2}+\frac{\pi}{3}\right)$
$=4 \sqrt{3}-4-\frac{\pi}{3}$
22. If $f$ and $g$ are differentiable functions in $[0,1]$ satisfying $f(0)=2=g(1), g(0)=0$ and $f(1)=6$, then for some $c \in] 0,1[$
(1) $2 f^{\prime}(c)=3 g^{\prime}(c)$
(2) $f^{\prime}(c)=g^{\prime}(c)$
(3) $f^{\prime}(c)=2 g^{\prime}(c)$
(4) $2 f^{\prime}(c)=g^{\prime}(c)$

## Answer (3)

Sol. Using, mean value theorem

$$
\begin{aligned}
& f^{\prime}(c)=\frac{f(1)-f(0)}{1-0}=4 \\
& g^{\prime}(c)=\frac{g(1)-g(0)}{1-0}=2
\end{aligned}
$$

so, $f^{\prime}(c)=2 g^{\prime}(c)$
23. If $g$ is the inverse of a function $f$ and $f^{\prime}(x)=\frac{1}{1+x^{5}}$, then $g^{\prime}(x)$ is equal to
(1) $5 x^{4}$
(2) $\frac{1}{1+\{g(x)\}^{5}}$
(3) $1+\{g(x)\}^{5}$
(4) $1+x^{5}$

Answer (3)
Sol. $f^{\prime}(x)=\frac{1}{1+x^{5}}=f(g(x))=x \rightarrow f^{\prime}(g(x)) g^{\prime}(x)=1$
$g^{\prime}(x)=\frac{1}{f^{\prime}(g(x))}=1+(g(x))^{5}$
24. If $(10)^{9}+2(11)^{1}(10)^{8}+3(11)^{2}(10)^{7}+\ldots+10(11)^{9}=$ $k(10)^{9}$, then $k$ is equal to
(1) $\frac{441}{100}$
(2) 100
(3) 110
(4) $\frac{121}{10}$

## Answer (2)

Sol. $10^{9}+2 \cdot(11)(10)^{8}+3(11)^{2}(10)^{7}+\ldots+10(11)^{9}=k(10)^{9}$
$x=10^{9}+2 \cdot(11)(10)^{8}+3(11)^{2}(10)^{7}+\ldots+10(11)^{9}$
$\frac{11}{10} x=11 \cdot 10^{8}+2 \cdot(11)^{2} \cdot(10)^{7}+\ldots+9(11)^{9}+11^{10}$

$$
\begin{aligned}
& x\left(1-\frac{11}{10}\right)=10^{9}+11(10)^{8}+11^{2} \times(10)^{7}+\ldots+11^{9}-11^{10} \\
& \left.\Rightarrow \quad-\frac{x}{10}=10^{9}\left(\frac{\left(\frac{11}{10}\right)^{10}-1}{\frac{11}{10}-1}\right)-11^{10}\right) \\
& \Rightarrow \quad-\frac{x}{10}=\left(11^{10}-10^{10}\right)-11^{10}=-10^{10} \\
& \Rightarrow x=10^{11}=k \cdot 10^{9} \\
& \Rightarrow k=100
\end{aligned}
$$

25. If $\alpha, \beta \neq 0$, and $f(n)=\alpha^{n}+\beta^{n}$ and
$\left|\begin{array}{ccc}3 & 1+f(1) & 1+f(2) \\ 1+f(1) & 1+f(2) & 1+f(3) \\ 1+f(2) & 1+f(3) & 1+f(4)\end{array}\right|$
$=K(1-\alpha)^{2}(1-\beta)^{2}(\alpha-\beta)^{2}$, then $K$ is equal to
(1) $\frac{1}{\alpha \beta}$
(2) 1
(3) -1
(4) $\alpha \beta$

## Answer (2)

Sol. $\left|\begin{array}{ccccccccc}1 & 1 & 1 & 1 & & & 1 & 2 & 2 \\ 1 & & & 1 & 2 & 2 & 1 & 3 & 3 \\ 1 & 2 & 2 & 1 & 3 & 3 & 1 & 4 & 4\end{array}\right|$

$$
\left|\begin{array}{lll}
1 & 1 & 1 \\
& & 1 \\
2 & 2 & 1
\end{array}\right|\left|\begin{array}{lll}
1 & & 2 \\
1 & & 2 \\
1 & 1 & 1
\end{array}\right|
$$

$=[(1-\alpha)(1-\beta)(1-\beta)]^{2}$
So, $k=1$
26. The slope of the line touching both the parabolas $y^{2}=4 x$ and $x^{2}=-32 y$ is
(1) $\frac{3}{2}$
(2) $\frac{1}{8}$
(3) $\frac{2}{3}$
(4) $\frac{1}{2}$

## Answer (4)

Sol. $y^{2}=4 x$
$x^{2}=-32 y$
$m$ be slope of common tangent
Equation of tangent (1)

$$
\begin{equation*}
y=m x+\frac{1}{m} \tag{i}
\end{equation*}
$$

Equation of tangent (2)

$$
\begin{equation*}
y=m x+8 m^{2} \tag{ii}
\end{equation*}
$$

(i) and (ii) are identical

$$
\begin{aligned}
& \frac{1}{m}=8 m^{2} \\
& \Rightarrow \quad m^{3}=\frac{1}{8} \\
& m=\frac{1}{2}
\end{aligned}
$$

## Alternative method :

Let tangent to $y^{2} \quad 4 x$ be

$$
y \quad m x \frac{1}{m}
$$

as this is also tangent to $x^{2} \quad 32 y$
Solving $x^{2} \quad 32 m x \quad \frac{32}{m} \quad 0$
Since roots are equal
$\therefore \quad D=0$

$$
(32)^{2} \quad 4 \quad \frac{32}{m} \quad 0
$$

$m^{3} \quad \frac{4}{32}$
m $\frac{1}{2}$
27. The statement $\sim(p \leftrightarrow \sim q)$ is
(1) Equivalent to $\sim p \leftrightarrow q$
(2) A tautology
(3) A fallacy
(4) Equivalent to $p \leftrightarrow q$

Answer (4)
Sol. $\sim(p \leftrightarrow \sim q)$

| $p$ | $q$ | $\sim q$ | $p \leftrightarrow \sim q$ | $\sim(p \leftrightarrow \sim q)$ |
| :---: | :---: | :---: | :---: | :---: |
| F | F | T | F | T |
| F | T | F | T | F |
| T | F | T | T | F |
| T | T | F | F | T |

Clearly equivalent to $p \leftrightarrow q$
28. Let the population of rabbits surviving at a time $t$ be governed by the differential equation $\frac{d p(t)}{d t}=\frac{1}{2} p(t)-200$. If $p(0)=100$, then $p(\mathrm{t})$ equals
(1) $300-200 e^{-t / 2}$
(2) $600-500 e^{t / 2}$
(3) $400-300 e^{-t / 2}$
(4) $400-300 e^{t / 2}$

## Answer (4)

Sol. $\frac{d p(t)}{d t}=\frac{1}{2} p(t)-200$
$\int \frac{d(p(t))}{\left(\frac{1}{2} p(t)-200\right)}=\int d t$
$2 \log \left(\frac{p(t)}{2}-200\right)=t+c$
$\frac{p(t)}{2}-200=e^{\frac{t}{2}} k$
29. Let $C$ be the circle with centre at $(1,1)$ and radius $=1$. If $T$ is the circle centred at $(0, y)$, passing through origin and touching the circle $C$ externally, then the radius of $T$ is equal to
(1) $\frac{\sqrt{3}}{2}$
(2) $\frac{1}{2}$
(3) $\frac{1}{4}$
(4) $\frac{\sqrt{3}}{\sqrt{2}}$

Answer (3)
Sol.

$C \equiv(x-1)^{2}+(y-1)^{2}=1$
Radius of $T=|y|$
$T$ touches $C$ externally
$(0-1)^{2}+(y-1)^{2}=(1+|y|)^{2}$
$\Rightarrow 1+y^{2}+1-2 y=1+y^{2}+2|y|$
If $y>0$,
$y^{2}+2-2 y=y^{2}+1+2 y$
$\Rightarrow 4 y=1$
$\Rightarrow y=\frac{1}{4}$
If $y<0$,
$y^{2}+2-2 y=y^{2}+1-2 y$
$\Rightarrow 1=2$ (Not possible)
$\therefore \quad y=\frac{1}{4}$
30. The angle between the lines whose direction cosines satisfy the equations $l+m+n=0$ and $l^{2}=m^{2}+n^{2}$ is
(1) $\frac{\pi}{4}$
(2) $\frac{\pi}{6}$
(3) $\frac{\pi}{2}$
(4) $\frac{\pi}{3}$

Answer (4)
Sol. $l+m+n=0$
$l^{2}=m^{2}+n^{2}$
Now, $(-m-n)^{2}=m^{2}+n^{2}$
$\Rightarrow m n=0$

$$
m=0 \text { or } n=0
$$

If $m=0$
then $l=-n$
$l^{2}+m^{2}+n^{2}=1$
Gives
$\Rightarrow n= \pm \frac{1}{\sqrt{2}}$
i.e. $\left(l_{1}, m_{1}, n_{1}\right)$

$$
=\left(-\frac{1}{\sqrt{2}}, 0, \frac{1}{\sqrt{2}}\right)
$$

If $n=0$
then $l=-m$
$l^{2}+m^{2}+n^{2}=1$
$\Rightarrow 2 m^{2}=1$
$\Rightarrow m^{2}=\frac{1}{2}$
$\Rightarrow m= \pm \frac{1}{\sqrt{2}}$
Let $m=\frac{1}{\sqrt{2}}$
$l=-\frac{1}{\sqrt{2}}$
$n=0$
$\left(l_{2}, m_{2}, n_{2}\right)$

$$
=\left(-\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}, 0\right)
$$

$\therefore \quad \cos \theta=\frac{1}{2}$

$$
\theta=\frac{\pi}{3}
$$

## PART-B : PHYSICS

31. When a rubber-band is stretched by a distance $x$, it exerts a restoring force of magnitude $F=a x+b x^{2}$ where $a$ and $b$ are constants. The work done in stretching the unstretched rubber-band by $L$ is
(1) $\frac{1}{2} \frac{a L^{2}}{2} \frac{b L^{3}}{3}$
(2) $a L^{2}+b L^{3}$
(3) $\frac{1}{2}\left(a L^{2} \quad b L^{3}\right)$
(4) $\frac{a L^{2}}{2} \quad \frac{b L^{3}}{3}$

## Answer (4)

Sol. $d W \quad F d l$

$$
\text { W } \begin{gathered}
{ }_{0}^{L} a x d x{ }_{0}^{L} b x^{2} d x \\
\frac{a L^{2}}{2} \frac{b L^{3}}{3} .
\end{gathered}
$$

32. The coercivity of a small magnet where the ferromagnet gets demagnetized is $3 \times 10^{3} \mathrm{Am}^{-1}$. The current required to be passed in a solenoid of length 10 cm and number of turns 100, so that the magnet gets demagnetized when inside the solenoid, is
(1) 6 A
(2) 30 mA
(3) 60 mA
(4) 3 A

## Answer (4)

Sol. $B=\mu_{0} n i$
$\frac{B}{0} n i$
$310^{3} \quad \frac{N I}{L} \quad \frac{100 \quad i}{10 \quad 10^{2}}$
$I=3 \mathrm{~A}$.
33. In a large building, there are 15 bulbs of 40 W , 5 bulbs of $100 \mathrm{~W}, 5$ fans of 80 W and 1 heater of 1 kW . The voltage of the electric mains is 220 V . The minimum capacity of the main fuse of the building will be
(1) 14 A
(2) 8 A
(3) 10 A
(4) 12 A

Answer (4)
Sol. $15 \times 40+5 \times 100+5 \times 80+1000=V \times I$
$600+500+400+1000=220 I$
I $\quad \frac{2500}{220} \quad 11.36$
$I=12$ A.
34. An open glass tube is immersed in mercury in such a way that a length of 8 cm extends above the mercury level. The open end of the tube is then closed and sealed and the tube is raised vertically up by additional 46 cm . What will be length of the air column above mercury in the tube now?
(Atmospheric pressure $=76 \mathrm{~cm}$ of Hg )
(1) 6 cm
(2) 16 cm
(3) 22 cm
(4) 38 cm

Answer (2)
Sol.

$P+x=P_{0}$
$P=(76-x)$
$8 \times A \times 76=(76-x) \times A \times(54-x)$
$x=38$
Length of air column $=54-38=16 \mathrm{~cm}$.
35. A bob of mass $m$ attached to an inextensible string of length $l$ is suspended from a vertical support. The bob rotates in a horizontal circle with an angular speed $\omega \mathrm{rad} / \mathrm{s}$ about the vertical. About the point of suspension
(1) Angular momentum changes both in direction and magnitude
(2) Angular momentum is conserved
(3) Angular momentum changes in magnitude but not in direction
(4) Angular momentum changes in direction but not in magnitude

## Answer (4)

Sol. $\tau=m g \times l \sin \theta$. (Direction parallel to plane of rotation of particle)

as $\tau$ is perpendicular to $\vec{L}$, direction of $L$ changes but magnitude remains same.
36. The current voltage relation of diode is given by $I=\left(e^{1000 \mathrm{~V} / \mathrm{T}}-1\right) \mathrm{mA}$, where the applied $V$ is in volts and the temperature $T$ is in degree kelvin. If a student makes an error measuring $\pm 0.01 \mathrm{~V}$ while measuring the current of 5 mA at 300 K , what will be the error in the value of current in mA ?
(1) 0.05 mA
(2) 0.2 mA
(3) 0.02 mA
(4) 0.5 mA

## Answer (2)

Sol. $I=\left(e^{1000 \mathrm{~V} / \mathrm{T}}-1\right) \mathrm{mA}$
When $I=5 \mathrm{~mA}, e^{1000 \mathrm{~V} / \mathrm{T}}=6 \mathrm{~mA}$
Also, $d I=\left(e^{1000 V / T}\right) \times \frac{1000}{T} \cdot d V$

$$
\begin{aligned}
& =(6 \mathrm{~mA}) \times \frac{1000}{300} \times(0.01) \\
& =0.2 \mathrm{~mA}
\end{aligned}
$$

37. From a tower of height $H$, a particle is thrown vertically upwards with a speed $u$. The time taken by the particle, to hit the ground, is $n$ times that taken by it to reach the highest point of its path. The relation between $H, u$ and $n$ is:
(1) $g H=(n-2) u^{2}$
(2) $2 g H=n^{2} u^{2}$
(3) $g H=(n-2)^{2} u^{2}$
(4) $2 g H=n u^{2}(n-2)$

## Answer (4)

Sol. Time taken to reach highest point is $t_{1}=\frac{u}{g}$ Speed on reaching ground $=\sqrt{u^{2}+2 g h}$

$$
\text { Now, } v=u+a t
$$

$\Rightarrow \sqrt{u^{2}+2 g h}=-u+g t$
$\Rightarrow t=\frac{u+\sqrt{u^{2}+2 g H}}{g}=\frac{n u}{g}$
$\Rightarrow \quad 2 g H=n(n-2) u^{2}$

38. A thin convex lens made from crown glass $\left(\mu=\frac{3}{2}\right)$ has focal length $f$. When it is measured in two different liquids having refractive indices $\frac{4}{3}$ and $\frac{5}{3}$, it has the focal lengths $f_{1}$ and $f_{2}$ respectively. The correct relation between the focal lengths is
(1) $f_{1}$ and $f_{2}$ both become negative
(2) $f_{1}=f_{2}<f$
(3) $f_{1}>f$ and $f_{2}$ becomes negative
(4) $f_{2}>f$ and $f_{1}$ becomes negative

## Answer (3)

Sol. By Lens maker's formula
$\frac{1}{f_{1}}=\left(\frac{3 / 2}{4 / 3}-1\right)\left(\frac{1}{R_{1}}-\frac{1}{R_{2}}\right)$
$\frac{1}{f_{2}}=\left(\frac{3 / 2}{5 / 3}-1\right)\left(\frac{1}{R_{1}}-\frac{1}{R_{2}}\right)$
$\frac{1}{f}=\left(\frac{3}{2}-1\right)\left(\frac{1}{R_{1}}-\frac{1}{R_{2}}\right)$
$\Rightarrow f_{1}=4 f \& f_{2}=-5 f$
39. A parallel plate capacitor is made of two circular plates separated by a distance 5 mm and with a dielectric of dielectric constant 2.2 between them. When the electric field in the dielectric is $3 \times 10^{4}$ $\mathrm{V} / \mathrm{m}$, the charge density of the positive plate will be close to
(1) $6 \times 10^{4} \mathrm{C} / \mathrm{m}^{2}$
(2) $6 \times 10^{-7} \mathrm{C} / \mathrm{m}^{2}$
(3) $3 \times 10^{-7} \mathrm{C} / \mathrm{m}^{2}$
(4) $3 \times 10^{4} \mathrm{C} / \mathrm{m}^{2}$

Answer (2)
Sol. $E=\frac{\sigma}{K \varepsilon_{0}}$

$$
\begin{aligned}
\sigma & =K \varepsilon_{0} E \\
& =2.2 \times 8.85 \times 10^{-12} \times 3 \times 10^{4} \approx 6 \times 10^{-7} \mathrm{C} / \mathrm{m}^{2}
\end{aligned}
$$

40. In the circuit shown here, the point ' $C$ ' is kept connected to point ' $A$ ' till the current flowing through the circuit becomes constant. Afterward, suddenly, point ' $C$ ' is disconnected from point ' $A$ ' and connected to point ' $B$ ' at time $t=0$. Ratio of the voltage across resistance and the inductor at $t=L / R$ will be equal to

(1) $\frac{1-e}{e}$
(2) $\frac{e}{1-e}$
(3) 1
(4) -1

Answer (4)
Sol. Applying Kirchhoff's law in closed loop, $-V_{R}-V_{C}=0$ $\Rightarrow V_{R} / V_{C}=-1$

Note : The sense of voltage drop has not been defined. The answer could have been 1 .
41. Two beams, $A$ and $B$, of plane polarized light with mutually perpendicular planes of polarization are seen through a polaroid. From the position when the beam $A$ has maximum intensity (and beam $B$ has zero intensity), a rotation of polaroid through $30^{\circ}$ makes the two beams appear equally bright. If the initial intensities of the two beams are $I_{A}$ and $I_{B}$ respectively, then $\frac{I_{A}}{I_{B}}$ equals
(1) $\frac{1}{3}$
(2) 3
(3) $\frac{3}{2}$
(4) 1

## Answer (1)

Sol. By law of Malus, $I=I_{0} \cos ^{2} \theta$
Now, $I_{A^{\prime}}=I_{A} \cos ^{2} 30$
$I_{B^{\prime}}=I_{B} \cos ^{2} 60$
As $I_{A^{\prime}}=I_{B^{\prime}}$
$\Rightarrow \quad I_{A} \times \frac{3}{4}=I_{B} \times \frac{1}{4}$

$$
\frac{I_{A}}{I_{B}}=\frac{1}{3}
$$

42. There is a circular tube in a vertical plane. Two liquids which do not mix and of densities $d_{1}$ and $d_{2}$ are filled in the tube. Each liquid subtends $90^{\circ}$ angle at centre. Radius joining their interface makes an angle $\alpha$ with vertical. Ratio $\frac{d_{1}}{d_{2}}$ is

(1) $\frac{1+\sin \alpha}{1-\cos \alpha}$
(2) $\frac{1+\sin \alpha}{1-\sin \alpha}$
(3) $\frac{1+\cos \alpha}{1-\cos \alpha}$
(4) $\frac{1+\tan \alpha}{1-\tan \alpha}$

## Answer (4)

Sol. Equating pressure at $A$

$(R \cos \alpha+R \sin \alpha) d_{2} g=(R \cos \alpha-R \sin \alpha) d_{1} g$
$\Rightarrow \frac{d_{1}}{d_{2}}=\frac{\cos \alpha+\sin \alpha}{\cos \alpha-\sin \alpha}=\frac{1+\tan \alpha}{1-\tan \alpha}$
43. The pressure that has to be applied to the ends of a steel wire of length 10 cm to keep its length constant when its temperature is raised by $100^{\circ} \mathrm{C}$ is
(For steel Young's modulus is $2 \times 10^{11} \mathrm{Nm}^{-2}$ and coefficient of thermal expansion is $1.1 \times 10^{-5} \mathrm{~K}^{-1}$ )
(1) $2.2 \times 10^{6} \mathrm{~Pa}$
(2) $2.2 \times 10^{8} \mathrm{~Pa}$
(3) $2.2 \times 10^{9} \mathrm{~Pa}$
(4) $2.2 \times 10^{7} \mathrm{~Pa}$

Answer (2)
Sol. As length is constant,
Strain $=\frac{\Delta L}{L}=\alpha \Delta Q$
Now pressure $=$ stress $=Y \times$ strain

$$
\begin{aligned}
& =2 \times 10^{11} \times 1.1 \times 10^{-5} \times 100 \\
& =2.2 \times 10^{8} \mathrm{~Pa}
\end{aligned}
$$

44. A block of mass $m$ is placed on a surface with a vertical cross-section given by $y=\frac{x^{3}}{6}$. If the coefficient of friction is 0.5 , the maximum height above the ground at which the block can be placed without slipping is
(1) $\frac{1}{2} \mathrm{~m}$
(2) $\frac{1}{6} \mathrm{~m}$
(3) $\frac{2}{3} \mathrm{~m}$
(4) $\frac{1}{3} \mathrm{~m}$

## Answer (2)

Sol. $\tan \theta=\frac{d y}{d x}=\frac{x^{2}}{2}$
At limiting equilibrium,

$$
\begin{aligned}
\mu & =\tan \theta \\
0.5 & =\frac{x^{2}}{2} \\
\Rightarrow \quad x & = \pm 1
\end{aligned}
$$

Now, $y=\frac{1}{6}$
45. Three rods of copper, brass and steel are welded together to form a Y-shaped structure. Area of crossseciton of each rod $=4 \mathrm{~cm}^{2}$. End of copper rod is maintained at $100^{\circ} \mathrm{C}$ whereas ends of brass and steel are kept at $0^{\circ} \mathrm{C}$. Lengths of the copper, brass
and steel rods are 46,13 and 12 cm respectively. The rods are thermally insulated from surroundings except at ends. Thermal conductivities of copper, brass and steel are $0.92,0.26$ and 0.12 CGS units respectively. Rate of heat flow through copper rod is
(1) $6.0 \mathrm{cal} / \mathrm{s}$
(2) $1.2 \mathrm{cal} / \mathrm{s}$
(3) $2.4 \mathrm{cal} / \mathrm{s}$
(4) $4.8 \mathrm{cal} / \mathrm{s}$

## Answer (4)

Sol.


$$
\begin{aligned}
Q= & Q_{1}+Q_{2} \\
& \frac{0.92 \times 4(100-T)}{46}=\frac{0.26 \times 4 \times(T-0)}{13}+\frac{0.12 \times 4 \times T}{12}
\end{aligned}
$$

$$
\Rightarrow \quad 200-2 T=2 T+T
$$

$$
\Rightarrow \quad T=40^{\circ} \mathrm{C}
$$

$$
\Rightarrow Q=\frac{0.92 \times 4 \times 60}{46}=4.8 \mathrm{cal} / \mathrm{s}
$$

46.. A mass $m$ is supported by a massless string wound around a uniform hollow cylinder of mass $m$ and radius $R$. If the string does not slip on the cylinder, with what acceleration will the mass fall on release?

(1) $g$
(2) $\frac{2 g}{3}$
(3) $\frac{g}{2}$
(4) $\frac{5 g}{6}$

## Answer (3)

Sol. $a=R \alpha$
$m g-T=m a$
$T \times R=m R^{2} \alpha$
or $T=m a$
$\Rightarrow a=\frac{g}{2}$
47. Match List-I (Electromagnetic wave type) with List - II (Its association/application) and select the correct option from the choices given below the lists

| List-I |  | List-II |  |
| :--- | :--- | :--- | :--- |
| (a) | Infrared waves | (i) | To treat muscular <br> strain |
| (c) | Radio waves | (ii) | For broadcasting |
| (d) | Ultraviolet <br> rays | (iii) | To detect fracture <br> of bones <br> Absorbed by the <br> ozone layer of the <br> atmosphere |

(1) (i) (ii)
(b)
(c) (d)
(iii) (iv)
(2) (iv)
(iii)
(ii) (i)
(3) (i)
(ii)
(iv) (iii)
(4) (iii)
(ii)
(i) (iv)

## Answer (1)

Sol. (a) Infrared rays are used to treat muscular strain
(b) Radiowaves are used for broadcasting
(c) X-rays are used to detect fracture of bones
(d) Ultraviolet rays are absorbed by ozone
48. The radiation corresponding to $3 \rightarrow 2$ transition of hydrogen atoms falls on a metal surface to produce photoelectrons. These electrons are made to enter a magnetic field of $3 \times 10^{-4} \mathrm{~T}$. If the radius of the largest circular path followed by these electrons is 10.0 mm , the work function of the metal is close to
(1) 1.6 eV
(2) 1.8 eV
(3) 1.1 eV
(4) 0.8 eV

Answer (3)
Sol. $r=\frac{m v}{q B}=\frac{\sqrt{2 m e V}}{e B}=\frac{1}{B} \sqrt{\frac{2 m}{e} V}$

$$
\Rightarrow \quad V=\frac{B^{2} r^{2} e}{2 m}=0.8 \mathrm{~V}
$$

For transition between 3 to 2,

$$
\begin{aligned}
& \begin{aligned}
E & =13.6\left(\frac{1}{4}-\frac{1}{9}\right) \\
& =\frac{13.6 \times 5}{36} \\
= & 1.88 \mathrm{eV}
\end{aligned} \\
& \text { Work function }
\end{aligned}
$$

49. During the propagation of electromagnetic waves in a medium
(1) Both electric and magnetic energy densities are zero
(2) Electric energy density is double of the magnetic energy density
(3) Electric energy density is half of the magnetic energy density
(4) Electric energy density is equal to the magnetic energy density

## Answer (4)

Sol. Energy is equally divided between electric and magnetic field
50. A green light is incident from the water to the air water interface at the critical angle( $\theta)$. Select the correct statement
(1) The entire spectrum of visible light will come out of the water at various angles to the normal
(2) The entire spectrum of visible light will come out of the water at an angle of $90^{\circ}$ to the normal
(3) The spectrum of visible light whose frequency is less than that of green light will come out to the air medium
(4) The spectrum of visible light whose frequency is more than that of green light will come out to the air medium

## Answer (3)

Sol. $\sin \theta_{c}=\frac{1}{\mu}$


For greater wavelength (i.e. lesser frequency) $\mu$ is less So, $\theta_{c}$ would be more. So, they will not suffer reflection and come out at angles less then $90^{\circ}$.
51. Four particles, each of mass $M$ and equidistant from each other, move along a circle of radius $R$ under the action of their mutual gravitational attraction. The speed of each particle is
(1) $\left.\frac{1}{2} \sqrt{\frac{G M}{R}(1} 22 \sqrt{2}\right)$
(2) $\sqrt{\frac{G M}{R}}$
(3) $\sqrt{2 \sqrt{2} \frac{G M}{R}}$
(4) $\left.\sqrt{\frac{G M}{R}(1} 22 \sqrt{2}\right)$

Answer (1)

Sol. $\frac{F}{\sqrt{2}}+\frac{F}{\sqrt{2}}+F^{\prime}=\frac{m v^{2}}{R}$

$$
\begin{aligned}
& \frac{2 \times G m^{2}}{\sqrt{2}(R \sqrt{2})^{2}}+\frac{G m^{2}}{4 R^{2}}=\frac{m v^{2}}{R} \\
& \frac{G m^{2}}{R}\left[\frac{1}{4}+\frac{1}{\sqrt{2}}\right]=m v^{2} \\
& v=\sqrt{\frac{G m}{R}\left(\frac{\sqrt{2}+4}{4 \sqrt{2}}\right)} \\
& =\frac{1}{2} \sqrt{\frac{G m}{R}(1+2 \sqrt{2})}
\end{aligned}
$$

52. A particle moves with simple harmonic motion in a straight line. In first $\tau \mathrm{s}$, after starting from rest it travels a distance $a$, and in next $\tau$ s it travels $2 a$ in same direction then
(1) Time period of oscillations is $6 \tau$
(2) Amplitude of motion is $3 a$
(3) Time period of oscillations is $8 \tau$
(4) Amplitude of motion is $4 a$

## Answer (1)

Sol. As it starts from rest, we have
$x=A \cos \omega t$. At $t=0, x=A$
when $t=\tau, x=A-a$
when $t=2 \tau, x=A-3 a$
$\Rightarrow A-a=A \cos \omega \tau$

$$
A-3 a=A \cos 2 \omega \tau
$$

As $\cos 2 \omega \tau=2 \cos ^{2} \omega \tau-1$
$\Rightarrow \frac{A-3 a}{A}=2\left(\frac{A-a}{A}\right)^{2}-1$

$$
\begin{aligned}
& \quad \frac{A-3 a}{A}=\frac{2 A^{2}+2 a^{2}-4 A a-A^{2}}{A^{2}} \\
& A^{2}-3 a A=A^{2}+2 a^{2}-4 A a \\
& a^{2}=2 a A \\
& A=
\end{aligned}
$$

Now, $A-a=A \cos \omega \tau$
$\Rightarrow \quad \cos \omega \tau=\frac{1}{2}$

$$
\frac{2 \pi}{T} \tau=\frac{\pi}{3}
$$

$$
\Rightarrow \quad T=6 \tau
$$

53. A conductor lies along the $z$-axis at $-1.5 \leq z<1.5 \mathrm{~m}$ and carries a fixed current of 10.0 A in $-\hat{a}_{z}$ direction (see figure). For a field $\vec{B} \quad 3.0 \quad 10^{4} e^{-0.2 x} \hat{a}_{y} T$, find the power required to move the conductor at constant speed to $x=2.0 \mathrm{~m}, y=0 \mathrm{~m}$ in $5 \times 10^{-3} \mathrm{~s}$. Assume parallel motion along the $x$-axis

(1) 29.7 W
(2) 1.57 W
(3) 2.97 W
(4) 14.85 W

## Answer (3)

Sol. Average Power $=\frac{\text { work }}{\text { time }}$

$$
\begin{aligned}
W & =\int_{0}^{2} F d x \\
& =\int_{0}^{2} 3.0 \times 10^{-4} e^{-0.2 x} \times 10 \times 3 d x \\
& =9 \times 10^{-3} \int_{0}^{2} e^{-0.2 x} d x \\
& =\frac{9 \times 10^{-3}}{0.2}\left[-e^{-0.2 \times 2}+1\right] \quad B=3.0 \times 10^{-4} e^{-0.2 x} \\
& =\frac{9 \times 10^{-3}}{0.2} \times\left[1-e^{-0.4}\right] \\
& =9 \times 10^{-3} \times(0.33) \\
& =2.97 \times 10^{-3} \mathrm{~J} \\
P & =\frac{2.97 \times 10^{-3}}{(0.2) \times 5 \times 10^{-3}}=2.97 \mathrm{~W}
\end{aligned}
$$

54. The forward biased diode connection is
(1) $\xrightarrow{-2 \mathrm{~V}}$ - Wunい- +2 V
(2) $\xrightarrow{+2 \mathrm{~V}} \longrightarrow$ ——wnu- -2 V
(3) $\xrightarrow{-3 \mathrm{~V}}$ வ Munu- -3 V
(4) $\xrightarrow{2 \mathrm{~V}}$ 人 $\mathrm{MuMr}^{4} \mathrm{~V}$

Answer (2)

Sol.


For forward Bias, $p$-side must be at higher potential than $n$-side.
55. Hydrogen $\left({ }_{1} \mathrm{H}^{1}\right)$, Deuterium $\left({ }_{1} \mathrm{H}^{2}\right)$, singly ionised Helium $\left({ }_{2} \mathrm{He}^{4}\right)^{+}$and doubly ionised lithium $\left({ }_{3} \mathrm{Li}^{6}\right)^{++}$ all have one electron around the nucleus. Consider an electron transition from $n=2$ to $n=1$. If the wave lengths of emitted radiation are $\lambda_{1}, \lambda_{2}, \lambda_{3}$ and $\lambda_{4}$ respectively then approximately which one of the following is correct?
(1) $\lambda_{1}=2 \lambda_{2}=3 \lambda_{3}=4 \lambda_{4}$
(2) $4 \lambda_{1}=2 \lambda_{2}=2 \lambda_{3}=\lambda_{4}$
(3) $\lambda_{1}=2 \lambda_{2}=2 \lambda_{3}=\lambda_{4}$
(4) $\lambda_{1}=\lambda_{2}=4 \lambda_{3}=9 \lambda_{4}$

Answer (4)
Sol. $\frac{1}{\lambda}=R Z^{2}\left[\frac{1}{n_{1}^{2}}-\frac{1}{n^{2}}\right]$
$\Rightarrow \lambda \propto \frac{1}{Z^{2}}$ for given $n_{1} \& n_{2}$

$$
\Rightarrow \lambda_{1}=\lambda_{2}=4 \lambda_{3}=9 \lambda_{4}
$$

56. On heating water, bubbles being formed at the bottom of the vessel detatch and rise. Take the bubbles to be spheres of radius $R$ and making a circular contact of radius $r$ with the bottom of the vessel. If $r \ll R$, and the surface tension of water is $T$, value of $r$ just before bubbles detatch is (Density of water is $\rho_{w}$ )

(1) $R^{2} \sqrt{\frac{3 \rho_{w} g}{T}}$
(2) $R^{2} \sqrt{\frac{\rho_{w} g}{3 T}}$
(3) $R^{2} \sqrt{\frac{\rho_{w} g}{6 T}}$
(4) $R^{2} \sqrt{\frac{\rho_{w} g}{T}}$

## Answer (No answer)

Sol. When the bubble gets detached,
Buoyant force $=$ force due to surface tension

$\int T \times d l \sin \theta=\frac{4}{3} \pi R^{3} \rho_{w} g$
$\Rightarrow \quad T \times 2 \pi r \times \frac{r}{R}=\frac{4}{3} \pi R^{3} \rho_{w} g$
$\Rightarrow \quad r^{2}=\frac{2 R^{4} \rho_{w} g}{3}$
$\Rightarrow \quad r=R^{2} \sqrt{\frac{2 \rho_{w} g}{3 T}}$
57. A pipe of length 85 cm is closed from one end. Find the number of possible natural oscillations of air column in the pipe whose frequencies lie below 1250 Hz . The velocity of sound in air is $340 \mathrm{~m} / \mathrm{s}$.
(1) 4
(2) 12
(3) 8
(4) 6

Answer (4)
Sol. $f=\frac{(2 n-1) v}{4 L} \leq 1250$
$\Rightarrow \frac{(2 n-1) \times 340}{0.85 \times 4} \leq 1250$
$\Rightarrow 2 n-1 \leq 12.5$
$\therefore \quad$ Answer is 6 .
58. Assume that an electric field $\vec{E}=30 x^{2} \hat{i}$ exists in space. Then the potential difference $V_{A}-V_{O}$, where $V_{O}$ is the potential at the origin and $V_{A}$ the potential at $x=2 \mathrm{~m}$ is
(1) 80 J
(2) 120 J
(3) -120 J
(4) -80 J

Answer (4)

Sol. $d V=-\vec{E} \cdot \overrightarrow{d x}$
$\int_{V_{0}}^{V_{A}} d V=-\int_{0}^{2} 30 x^{2} d x$
$V_{A}-V_{O}=-\left[10 x^{3}\right]_{0}^{2}=-80 \mathrm{~V}$
59. A student measured the length of a rod and wrote it as 3.50 cm . Which instrument did he use to measure it?
(1) A screw gauge having 50 divisions in the circular scale and pitch as 1 mm
(2) A meter scale
(3) A vernier calliper where the 10 divisions in vernier scale matches with 9 division in main scale and main scale has 10 divisions in 1 cm
(4) A screw gauge having 100 divisions in the circular scale and pitch as 1 mm

## Answer (3)

Sol. As measured value is 3.50 cm , the least count must be $0.01 \mathrm{~cm}=0.1 \mathrm{~mm}$

For vernier scale with $1 \mathrm{MSD}=1 \mathrm{~mm}$ and $9 \mathrm{MSD}=10 \mathrm{VSD}$,

$$
\begin{aligned}
\text { Least count } & =1 \mathrm{MSD}-1 \mathrm{VSD} \\
& =0.1 \mathrm{~mm}
\end{aligned}
$$

60. One mole of diatomic ideal gas undergoes a cyclic process $A B C$ as shown in figure. The process $B C$ is adiabatic. The temperatures at $A, B$ and $C$ are 400 K , 800 K and 600 K respectively. Choose the correct statement

(1) The change in internal energy in the process $B C$ is $-500 R$
(2) The change in internal energy in whole cyclic process is $250 R$
(3) The change in internal energy in the process $C A$ is 700 R
(4) The change in internal energy in the process $A B$ is $-350 R$

Answer (1)
Sol. $\Delta U=n C_{V} \Delta T=1 \times \frac{5 R}{2} \Delta T$
For $B C, \Delta T=-200 \mathrm{~K}$
$\Rightarrow \Delta U=-500 R$

## PART-C : CHEMISTRY

61. Which one is classified as a condensation polymer?
(1) Acrylonitrile
(2) Dacron
(3) Neoprene
(4) Teflon

## Answer (2)

Sol. Dacron is polyester formed by condensation polymerisation of terephthalic acid and ethylene glycol.


Acrylonitrile, Neoprene and Teflon are addition polymers of acrylonitrile, isoprene and tetrafluoro ethylene respectively.
62. Which one of the following properties is not shown by NO?
(1) It's bond order is 2.5
(2) It is diamagnetic in gaseous state
(3) It is a neutral oxide
(4) It combines with oxygen to form nitrogen dioxide

## Answer (2)

Sol. Nitric oxide is paramagnetic in the gaseous state as it has one unpaired electron in its outermost shell. The electronic configuration of NO is

$$
\sigma_{1 \mathrm{~s}}^{2} \sigma_{1 \mathrm{~s}}^{*^{2}} \sigma_{2 \mathrm{~s}}^{2} \sigma_{2 \mathrm{~s}}^{*^{2}} \sigma_{2 \mathrm{p}_{\mathrm{z}}}^{2} \pi_{2 p_{\mathrm{x}}}^{2}=\pi_{2 p_{\mathrm{y}}}^{2} \pi_{2 p_{\mathrm{x}}}^{*^{1}}
$$

However, it dimerises at low temperature to become diamagnetic.

$$
2 \mathrm{NO} \rightleftharpoons \mathrm{~N}_{2} \mathrm{O}_{2}
$$

Its bond order is 2.5 and it combines with $\mathrm{O}_{2}$ to give nitrogen dioxide.
63. Sodium phenoxide when heated with $\mathrm{CO}_{2}$ under pressure at $125^{\circ} \mathrm{C}$ yields a product which on acetylation produces C .


The major product $C$ would be
(1)

(2)

(3)

(4)


Answer (2)

Sol.


64. Given below are the half-cell reactions
$\mathrm{Mn}^{2+}+2 \mathrm{e}^{-} \rightarrow \mathrm{Mn} ; \mathrm{E}^{\circ}=-1.18 \mathrm{~V}$
$\left(\mathrm{Mn}^{3+}+\mathrm{e}^{-} \rightarrow \mathrm{Mn}^{2+}\right) ; \mathrm{E}^{\circ}=+1.51 \mathrm{~V}$
The $\mathrm{E}^{\circ}$ for $3 \mathrm{Mn}^{2+} \rightarrow \mathrm{Mn}+2 \mathrm{Mn}^{3+}$ will be
(1) -0.33 V ; the reaction will occur
(2) -2.69 V ; the reaction will not occur
(3) -2.69 V ; the reaction will occur
(4) -0.33 V ; the reaction will not occur

## Answer (2)

Sol. (1) $\mathrm{Mn}^{2+}+2 \mathrm{e} \rightarrow \mathrm{Mn} ; \mathrm{E}^{\circ}=-1.18 \mathrm{~V}$;

$$
\Delta \mathrm{G}_{1}^{\circ}=-2 \mathrm{~F}(-1.18)=2.36 \mathrm{~F}
$$

(2) $\mathrm{Mn}^{3+}+\mathrm{e} \rightarrow \mathrm{Mn}^{2+} ; \mathrm{E}^{\circ}=+1.51 \mathrm{~V}$;

$$
\Delta \mathrm{G}_{2}^{\circ}=-\mathrm{F}(1.51)=-1.51 \mathrm{~F}
$$

(1) $-2 \times(2)$
$3 \mathrm{Mn}^{2+} \rightarrow \mathrm{Mn}+2 \mathrm{Mn}^{3+}$;

$$
\begin{aligned}
\Delta \mathrm{G}_{3}^{\circ} & =\Delta \mathrm{G}_{1}^{\circ}-2 \Delta \mathrm{G}_{2}^{\circ} \\
& =[2.36-2(-1.51)] \mathrm{F} \\
& =(2.36+3.02) \mathrm{F} \\
& =5.38 \mathrm{~F}
\end{aligned}
$$

But $\Delta \mathrm{G}_{3}^{\circ}=-2 \mathrm{FE}^{\circ}$
$\Rightarrow 5.38 \mathrm{~F}=-2 \mathrm{FE}^{\circ}$
$\Rightarrow \mathrm{E}^{\circ}=-2.69 \mathrm{~V}$
As $E^{\circ}$ value is negative reaction is non spontaneous.
65. For complete combustion of ethanol,
$\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}(\mathrm{l})+3 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow 2 \mathrm{CO}_{2}(\mathrm{~g})+3 \mathrm{H}_{2} \mathrm{O}(\mathrm{l})$,
the amount of heat produced as measured in bomb calorimeter, is $1364.47 \mathrm{~kJ} \mathrm{~mol}^{-1}$ at $25^{\circ} \mathrm{C}$. Assuming ideality the enthalpy of combustion, $\Delta_{c} \mathrm{H}$, for the reaction will be $\left(\mathrm{R}=8.314 \mathrm{~kJ} \mathrm{~mol}^{-1}\right)$
(1) $-1350.50 \mathrm{~kJ} \mathrm{~mol}^{-1}$
(2) $-1366.95 \mathrm{~kJ} \mathrm{~mol}^{-1}$
(3) $-1361.95 \mathrm{~kJ} \mathrm{~mol}^{-1}$
(4) $-1460.50 \mathrm{~kJ} \mathrm{~mol}^{-1}$

## Answer (2)

Sol. $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}(\mathrm{l})+3 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow 2 \mathrm{CO}_{2}(\mathrm{~g})+3 \mathrm{H}_{2} \mathrm{O}(l)$
Bomb calorimeter gives $\Delta \mathrm{U}$ of the reaction
So, as per question

$$
\begin{aligned}
\Delta \mathrm{U} & =-1364.47 \mathrm{~kJ} \mathrm{~mol}^{-1} \\
\Delta \mathrm{n}_{\mathrm{g}} & =-1 \\
\Delta \mathrm{H} & =\Delta \mathrm{U}+\Delta \mathrm{n}_{\mathrm{g}} \mathrm{RT} \\
& =-1364.47-\frac{1 \times 8.314 \times 298}{1000} \\
& =-1366.93 \mathrm{~kJ} \mathrm{~mol}^{-1}
\end{aligned}
$$

66. For the estimation of nitrogen, 1.4 g of an organic compound was digested by Kjeldahl method and the evolved ammonia was absorbed in 60 mL of $\frac{\mathrm{M}}{10}$ sulphuric acid. The unreacted acid required 20 mL of $\frac{\mathrm{M}}{10}$ sodium hydroxide for complete neutralization. The percentage of nitrogen in the compound is
(1) $5 \%$
(2) $6 \%$
(3) $10 \%$
(4) $3 \%$

## Answer (3)

Sol. As per question

|  | Normality | Volume |
| :---: | :---: | :---: |
| $\mathrm{H}_{2} \mathrm{SO}_{4}$ | $\frac{\mathrm{~N}}{5}$ | 60 mL |
| NaOH | $\frac{\mathrm{N}}{10}$ | 20 mL |

$\left(\mathrm{n}_{\mathrm{geq}}\right)_{\mathrm{H}_{2} \mathrm{SO}_{4}}=\left(\mathrm{n}_{\mathrm{geq}}\right)_{\mathrm{NaOH}}+\left(\mathrm{n}_{\mathrm{geq}}\right)_{\mathrm{NH}_{3}}$
$\frac{1}{5} \times \frac{60}{1000}=\frac{1}{10} \times \frac{20}{1000}+\left(\mathrm{n}_{\text {geq }}\right)_{\mathrm{NH}_{3}}$
$\frac{6}{500}=\frac{1}{500}+\left(\mathrm{n}_{\mathrm{geq}}\right)_{\mathrm{NH}_{3}}$
$\left(\mathrm{n}_{\text {geq }}\right)_{\mathrm{NH}_{3}}=\frac{5}{500}=\frac{1}{100}$
$\left(\mathrm{n}_{\mathrm{mol}}\right)_{\mathrm{N}}=\left(\mathrm{n}_{\mathrm{mol}}\right)_{\mathrm{NH}_{3}}=\left(\mathrm{n}_{\mathrm{geq}}\right)_{\mathrm{NH}_{3}}=\frac{1}{100}$
$(\text { Mass })_{N}=\frac{14}{100}=0.14 \mathrm{~g}$

Percentage of "N" $=\frac{0.14}{1.4} \times 100=10 \%$
67. The major organic compound formed by the reaction of 1, 1, 1-trichloroethane with silver powder is
(1) 2-Butene
(2) Acetylene
(3) Ethene
(4) 2-Butyne

## Answer (4)

Sol.


[^0]68. The ratio of masses of oxygen and nitrogen in a particular gaseous mixture is $1: 4$. The ratio of number of their molecule is
(1) $3: 16$
(2) $1: 4$
(3) $7: 32$
(4) $1: 8$

Answer (3)
Sol. Let the mass of $\mathrm{O}_{2}=\mathrm{x}$

$$
\text { Mass of } N_{2}=4 x
$$

Number of moles of $\mathrm{O}_{2}=\frac{\mathrm{x}}{32}$
Number of moles of $\mathrm{N}_{2}=\frac{4 \mathrm{x}}{28}=\frac{x}{7}$
$\therefore \quad$ Ratio $=\frac{x}{32}: \frac{x}{7}=7: 32$
69. The metal that cannot be obtained by electrolysis of an aqueous solution of its salts is
(1) Cr
(2) Ag
(3) Ca
(4) Cu

## Answer (3)

Sol. On electrolysis only in case of $\mathrm{Ca}^{2+}$ salt aqueous solution $\mathrm{H}_{2}$ gas discharge at Cathode.

## Case of Cr

At cathode : $\mathrm{Cr}^{3+}+2 \mathrm{e}^{-} \longrightarrow \mathrm{Cr}$
So, Cr is deposited.

## Case of Ag

At cathode : $\mathrm{Ag}^{+}+\mathrm{e}^{-} \longrightarrow \mathrm{Ag}$
So, Ag is deposited.

## Case of Cu

At cathode : $\mathrm{Cu}^{2+}+2 \mathrm{e}^{-} \longrightarrow \mathrm{Cu}$
Case of $\mathrm{Ca}^{2+}$
At cathode : $\mathrm{H}_{2} \mathrm{O}+\mathrm{e}^{-} \longrightarrow \frac{1}{2} \mathrm{H}_{2}+\mathrm{OH}^{-}$
70. The equivalent conductance of NaCl at concentration C and at infinite dilution are $\lambda_{\mathrm{C}}$ and $\lambda_{\infty}$ respectively. The correct relationship between $\lambda_{C}$ and $\lambda_{\infty}$ is given as
(Where the constant B is positive)
(1) C
(B) $\sqrt{C}$
(2) C
(B) C
(3) $\quad \mathrm{C} \quad-(\mathrm{B}) \mathrm{C}$
(4) $\quad$ C $\quad-(B) \sqrt{C}$

## Answer (4)

Sol. According to Debye Huckle onsager equation,

$$
\lambda_{C}=\lambda_{\infty}-A \sqrt{C}
$$

Here $\mathrm{A}=\mathrm{B}$
$\therefore \quad \lambda_{C}=\lambda_{\infty}-B \sqrt{C}$
71. The correct set of four quantum numbers for the valence electrons of rubidium atom $(Z=37)$ is
(1) $5,0,1,+\frac{1}{2}$
(2) $5,0,0,+\frac{1}{2}$
(3) $5,1,0,+\frac{1}{2}$
(4) $5,1,1,+\frac{1}{2}$

## Answer (2)

Sol. $37 \rightarrow 1 s^{2} 2 s^{2} 2 p^{6} 3 s^{2} 3 p^{6} 3 d^{10} 4 s^{2} 4 p^{6} 5 s^{1}$
So last electron enters $5 s$ orbital
Hence $\mathrm{n}=5, \mathrm{l}=0, \mathrm{~m}_{1}=0, \mathrm{~m}_{\mathrm{s}}= \pm \frac{1}{2}$
72. Consider separate solutions of $0.500 \mathrm{M} \mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}(\mathrm{aq})$, $0.100 \mathrm{M} \mathrm{Mg}_{3}\left(\mathrm{PO}_{4}\right)_{2}(\mathrm{aq}), 0.250 \mathrm{M} \mathrm{KBr}(\mathrm{aq})$ and 0.125 $\mathrm{M} \mathrm{Na}_{3} \mathrm{PO}_{4}(\mathrm{aq})$ at $25^{\circ} \mathrm{C}$. Which statement is true about these solutions, assuming all salts to be strong electrolytes?
(1) $0.500 \mathrm{M} \mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}(\mathrm{aq})$ has the highest osmotic pressure.
(2) They all have the same osmotic pressure.
(3) $0.100 \mathrm{M} \mathrm{Mg}_{3}\left(\mathrm{PO}_{4}\right)_{2}(\mathrm{aq})$ has the highest osmotic pressure.
(4) $0.125 \mathrm{M} \mathrm{Na}_{3} \mathrm{PO}_{4}(\mathrm{aq})$ has the highest osmotic pressure.

## Answer (2)

Sol. $\pi=\mathrm{i}$ CRT
$\pi_{\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}}=1 \times 0.500 \times \mathrm{R} \times \mathrm{T}=0.5 \mathrm{RT}$
$\pi_{\mathrm{Mg}_{3}\left(\mathrm{PO}_{4}\right)_{2}}=5 \times 0.100 \times \mathrm{R} \times \mathrm{T}=0.5 \mathrm{RT}$
$\begin{array}{llllll}\text { KBr } & 2 & 0.250 & \mathrm{R} & \mathrm{T} & 0.5 \mathrm{RT}\end{array}$
$\begin{array}{lllll}\mathrm{Na}_{3} \mathrm{PO}_{4} & 4 & 0.125 & \mathrm{RT} & 0.5 \mathrm{RT}\end{array}$
73. The most suitable reagent for the conversion of $\mathrm{R}-\mathrm{CH}_{2}-\mathrm{OH} \rightarrow \mathrm{R}-\mathrm{CHO}$ is
(1) PCC (Pyridinium Chlorochromate)
(2) $\mathrm{KMnO}_{4}$
(3) $\mathrm{K}_{2} \mathrm{Cr}_{2} \mathrm{O}_{7}$
(4) $\mathrm{CrO}_{3}$

## Answer (1)

Sol. PCC is mild oxidising agent, it will convert $\mathrm{R}-\mathrm{CH}_{2}-\mathrm{OH} \longrightarrow \mathrm{R}-\mathrm{CHO}$
74. CsCl crystallises in body centred cubic lattice. If ' a ' is its edge length then which of the following expressions is correct?
(1) $\mathrm{r}_{\mathrm{Cs}^{+}}+\mathrm{r}_{\mathrm{Cl}^{-}}=\sqrt{3} \mathrm{a}$
(2) $\mathrm{r}_{\mathrm{Cs}^{+}}+\mathrm{r}_{\mathrm{Cl}^{-}}=3 \mathrm{a}$
(3) $\mathrm{r}_{\mathrm{Cs}^{+}}+\mathrm{r}_{\mathrm{Cl}^{-}}=\frac{3 \mathrm{a}}{2}$
(4) $\mathrm{r}_{\mathrm{Cs}^{+}}+\mathrm{r}_{\mathrm{Cl}^{-}}=\frac{\sqrt{3}}{2} \mathrm{a}$

## Answer (4)

Sol.

$2 \mathrm{r}_{\mathrm{Cl}^{-}}+2 \mathrm{r}_{\mathrm{Cs}^{+}}=\sqrt{3} \mathrm{a}$
$\mathrm{r}_{\mathrm{Cl}^{-}}+\mathrm{r}_{\mathrm{Cs}^{+}}=\frac{\sqrt{3} \mathrm{a}}{2}$
75. In which of the following reactions $\mathrm{H}_{2} \mathrm{O}_{2}$ acts as a reducing agent?
(a) $\mathrm{H}_{2} \mathrm{O}_{2}+2 \mathrm{H}^{+}+2 \mathrm{e}^{-} \rightarrow 2 \mathrm{H}_{2} \mathrm{O}$
(b) $\mathrm{H}_{2} \mathrm{O}_{2}-2 \mathrm{e}^{-} \rightarrow \mathrm{O}_{2}+2 \mathrm{H}^{+}$
(c) $\mathrm{H}_{2} \mathrm{O}_{2}+2 \mathrm{e}^{-} \rightarrow 2 \mathrm{OH}^{-}$
(d) $\mathrm{H}_{2} \mathrm{O}_{2}+2 \mathrm{OH}^{-}-2 \mathrm{e}^{-} \rightarrow \mathrm{O}_{2}+2 \mathrm{H}_{2} \mathrm{O}$
(1) (b), (d)
(2) (a), (b)
(3) (c), (d)
(4) (a), (c)

Answer (1)
Sol. The reducing agent oxidises itself.
(a) $\mathrm{H}_{2} \mathrm{O}_{2}^{-1}+2 \mathrm{H}^{+}+2 \mathrm{e}^{-} \longrightarrow 2 \mathrm{H}_{2} \mathrm{O}^{-2}$
(b) $\mathrm{H}_{2} \mathrm{O}_{2}^{-1}-2 \mathrm{e} \longrightarrow \mathrm{O}_{2}^{0}+2 \mathrm{H}^{+}$
(c) $\mathrm{H}_{2} \mathrm{O}_{2}^{-1}+2 \mathrm{e} \longrightarrow 2 \mathrm{OH}^{-}$
(d) $\mathrm{H}_{2} \mathrm{O}_{2}^{-1}+2 \mathrm{OH}^{-}-2 \mathrm{e} \longrightarrow \mathrm{O}_{2}^{0}+\mathrm{H}_{2} \mathrm{O}$

Note : Powers of ' O ' are oxidation number of ' O ' in the compound.
76. For which of the following molecule significant $\mu \neq 0$ ?
(a)

(b)

(c)

(d)

(1) (c) and (d)
(2) Only (a)
(3) (a) and (b)
(4) Only (c)

Answer (1)

Sol. (a)

$\mu=0$
(c)

$\mu \neq 0$
(b)

$\mu=0$
,
(d)

$\mu \neq 0$
77. On heating an aliphatic primary amine with chloroform and ethanolic potassium hydroxide, the organic compound formed is
(1) An alkyl isocyanide
(2) An alkanol
(3) An alkanediol
(4) An alkyl cyanide

Answer (1)
Sol. $\mathrm{R}-\mathrm{CH}_{2}-\mathrm{NH}_{2} \xrightarrow[\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}]{\mathrm{CHCl}_{3} / \mathrm{KOH}} \mathrm{R}-\mathrm{CH}_{2}-\mathrm{NC}$
78. In $\mathrm{S}_{\mathrm{N}} 2$ reactions, the correct order of reactivity for the following compounds
$\mathrm{CH}_{3} \mathrm{Cl}, \mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{Cl},\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CHCl}$ and $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{CCl}$ is
(1) $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CHCl}>\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{Cl}>\mathrm{CH}_{3} \mathrm{Cl}>\left(\mathrm{CH}_{3}\right)_{3} \mathrm{CCl}$
(2) $\mathrm{CH}_{3} \mathrm{Cl}>\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CHCl}>\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{Cl}>\left(\mathrm{CH}_{3}\right)_{3} \mathrm{CCl}$
(3) $\mathrm{CH}_{3} \mathrm{Cl}>\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{Cl}>\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CHCl}>\left(\mathrm{CH}_{3}\right)_{3} \mathrm{CCl}$
(4) $\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{Cl}>\mathrm{CH}_{3} \mathrm{Cl}>\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CHCl}>\left(\mathrm{CH}_{3}\right)_{3} \mathrm{CCl}$

Aakash

Sol. Rate of $\mathrm{S}_{\mathrm{N}} 2$ reaction depends on steric crowding of alkyl halide. So order is
$\mathrm{CH}_{3} \mathrm{Cl}>\left(\mathrm{CH}_{3}\right) \mathrm{CH}_{2}-\mathrm{Cl}>\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CH}-\mathrm{Cl}>\left(\mathrm{CH}_{3}\right)_{3} \mathrm{CCl}$
79. The octahedral complex of a metal ion $\mathrm{M}^{3+}$ with four monodentate ligands $\mathrm{L}_{1}, \mathrm{~L}_{2}, \mathrm{~L}_{3}$ and $\mathrm{L}_{4}$ absorb wavelengths in the region of red, green, yellow and blue, respectively. The increasing order of ligand strength of the four ligands is
(1) $\mathrm{L}_{1}<\mathrm{L}_{2}<\mathrm{L}_{4}<\mathrm{L}_{3}$
(2) $\mathrm{L}_{4}<\mathrm{L}_{3}<\mathrm{L}_{2}<\mathrm{L}_{1}$
(3) $\mathrm{L}_{1}<\mathrm{L}_{3}<\mathrm{L}_{2}<\mathrm{L}_{4}$
(4) $\mathrm{L}_{3}<\mathrm{L}_{2}<\mathrm{L}_{4}<\mathrm{L}_{1}$

Answer (3)
Sol.


The energy of red light is less than that of violet light.
So energy order is
Red < Yellow < Green < Blue
The complex absorbs lower energy light lower will be its strength. So order of ligand strength is
$\mathrm{L}_{1}<\mathrm{L}_{3}<\mathrm{L}_{2}<\mathrm{L}_{4}$
80. The equation which is balanced and represents the correct product(s) is
(1) $\mathrm{CuSO}_{4}+4 \mathrm{KCN} \rightarrow \mathrm{K}_{2}\left[\mathrm{Cu}(\mathrm{CN})_{4}\right]+\mathrm{K}_{2} \mathrm{SO}_{4}$
(2) $\mathrm{Li}_{2} \mathrm{O}+2 \mathrm{KCl} \rightarrow 2 \mathrm{LiCl}+\mathrm{K}_{2} \mathrm{O}$
(3) $\left[\mathrm{CoCl}\left(\mathrm{NH}_{3}\right)_{5}\right]^{+}+5 \mathrm{H}^{+} \rightarrow \mathrm{Co}^{2+}+5 \mathrm{NH}_{4}^{+}+\mathrm{Cl}^{-}$
(4) $\left[\mathrm{Mg}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{2+}+(\text { EDTA })^{4-} \xrightarrow{\text { excess } \mathrm{NaOH}}$

$$
[\mathrm{Mg}(\text { EDTA })]^{2+}+6 \mathrm{H}_{2} \mathrm{O}
$$

## Answer (3)

Sol. The complex
$\left[\mathrm{CoCl}\left(\mathrm{NH}_{3}\right)_{5}\right]^{+}$decomposes under acidic medium, so
$\left[\mathrm{CoCl}\left(\mathrm{NH}_{3}\right)_{5}\right]^{+}+5 \mathrm{H}^{+} \rightarrow \mathrm{Co}^{2+}+5 \mathrm{NH}_{4}^{+}+\mathrm{Cl}^{-}$.
81. In the reaction,

the product C is
(1) Acetyl chloride
(2) Acetaldehyde
(3) Acetylene
(4) Ethylene

## Answer (4)

## Sol. Ethylene


82. The correct statement for the molecule, $\mathrm{CsI}_{3}$, is
(1) It contains $\mathrm{Cs}^{+}, \mathrm{I}^{-}$and lattice $\mathrm{I}_{2}$ molecule
(2) It is a covalent molecule
(3) It contains $\mathrm{Cs}^{+}$and $\mathrm{I}_{3}^{-}$ions
(4) It contains $\mathrm{Cs}^{3+}$ and $\mathrm{I}^{-}$ions

Answer (3)
Sol. It contains $\mathrm{Cs}^{+}$and $\mathrm{I}_{3}^{-}$ions
83. For the reaction $\mathrm{SO}_{2(\mathrm{~g})}+\frac{1}{2} \mathrm{O}_{2(\mathrm{~g})} \rightleftharpoons \mathrm{SO}_{3(\mathrm{~g})}$, if $K_{P}=K_{C}(R T)^{x}$ where the symbols have usual meaning then the value of $x$ is (assuming ideality)
(1) 1
(2) -1
(3) $-\frac{1}{2}$
(4) $\frac{1}{2}$

Answer (3)
Sol. $\mathrm{SO}_{2}(\mathrm{~g})+\frac{1}{2} \mathrm{O}_{2}(\mathrm{~g}) \rightleftharpoons \mathrm{SO}_{3}(\mathrm{~g})$
$K_{P}=K_{C}(R T)^{x}$
$\mathrm{x}=\Delta \mathrm{n}_{\mathrm{g}}=$ no. of gaseous moles in product

- no. of gaseous moles in reactant
$=1-\left(1+\frac{1}{2}\right)=1-\frac{3}{2}=\frac{-1}{2}$

84. For the non-stoichiometre reaction $2 \mathrm{~A}+\mathrm{B} \rightarrow \mathrm{C}+\mathrm{D}$, the following kinetic data were obtained in three separate experiments, all at 298 K .

| Initial <br> Concentration <br> $(A)$ | Initial <br> Concentration <br> $(B)$ | Initial rate of <br> formation of C <br> $\left(\mathrm{mol} \mathrm{L}^{-1} \mathrm{~s}^{-1}\right)$ |
| :--- | :--- | :--- |
| 0.1 M | 0.1 M | $1.2 \times 10^{-3}$ |
| 0.1 M | 0.2 M | $1.2 \times 10^{-3}$ |
| 0.2 M | 0.1 M | $2.4 \times 10^{-3}$ |

The rate law for the formation of C is
(1) $\frac{\mathrm{dc}}{\mathrm{dt}}=\mathrm{k}[\mathrm{A}]$
(2) $\frac{\mathrm{dc}}{\mathrm{dt}}=\mathrm{k}[\mathrm{A}][\mathrm{B}]$
(3) $\frac{\mathrm{dc}}{\mathrm{dt}}=\mathrm{k}[\mathrm{A}]^{2}[\mathrm{~B}]$
(4) $\frac{\mathrm{dc}}{\mathrm{dt}}=\mathrm{k}[\mathrm{A}][\mathrm{B}]^{2}$

## Answer (1)

Sol.
$2 \mathrm{~A}+\mathrm{B} \longrightarrow \mathrm{C}+\mathrm{D}$
Rate of Reaction $=\frac{-1}{2} \frac{\mathrm{~d}[\mathrm{~A}]}{\mathrm{dt}}=-\frac{\mathrm{d}[\mathrm{B}]}{\mathrm{dt}}$

$$
=\frac{\mathrm{d}[\mathrm{C}]}{\mathrm{dt}}=\frac{\mathrm{d}[\mathrm{D}]}{\mathrm{dt}}
$$

Let rate of Reaction $=\mathrm{k}[\mathrm{A}]^{\mathrm{x}}[\mathrm{B}]^{\mathrm{y}}$
Or, $\frac{\mathrm{d}[\mathrm{C}]}{\mathrm{dt}} \mathrm{k}[\mathrm{A}]^{\mathrm{x}}[\mathrm{B}]^{\mathrm{y}}$
Now from table,
$1.2 \times 10^{-3}=\mathrm{k}[0.1]^{\mathrm{x}}[0.1]^{\mathrm{y}}$
$1.2 \times 10^{-3}=\mathrm{k}[0.1]^{\mathrm{x}}[0.2]^{\mathrm{y}}$
$2.4 \times 10^{-3}=k[0.2]^{\mathrm{x}}[0.1]^{\mathrm{y}}$
Dividing equation (i) by (ii)
$\Rightarrow \quad \frac{1.210^{3}}{1.210^{3}} \frac{\mathrm{k}[0.1]^{\mathrm{x}}[0.1]^{\mathrm{y}}}{\mathrm{k}[0.1]^{\mathrm{x}}[0.2]^{\mathrm{y}}}$
$\Rightarrow \quad 1=\left[\frac{1}{2}\right]^{\mathrm{y}}$
$\Rightarrow \quad y=0$
Now Dividing equation (i) by (iii)

$$
\begin{aligned}
& \Rightarrow \quad \frac{1.210^{3}}{2.410^{3}} \frac{\mathrm{k}[0.1]^{\mathrm{x}}[0.1]^{\mathrm{y}}}{\mathrm{k}[0.2]^{\mathrm{x}}[0.1]^{\mathrm{y}}} \\
& \Rightarrow \quad\left[\frac{1}{2}\right]^{1}=\left[\frac{1}{2}\right]^{\mathrm{x}} \\
& \Rightarrow \quad \mathrm{x}=1
\end{aligned}
$$

Hence $\frac{\mathrm{d}[\mathrm{C}]}{\mathrm{dt}}=\mathrm{k}[\mathrm{A}]^{1}[\mathrm{~B}]^{0}$.
85. Resistance of 0.2 M solution of an electrolyte is $50 \Omega$. The specific conductance of the solution is $1.4 \mathrm{~S} \mathrm{~m}^{-1}$. The resistance of 0.5 M solution of the same electrolyte is $280 \Omega$. The molar conductivity of 0.5 M solution of the electrolyte in $\mathrm{S} \mathrm{m}^{2} \mathrm{~mol}^{-1}$ is
(1) $5 \times 10^{2}$
(2) $5 \times 10^{-4}$
(3) $5 \times 10^{-3}$
(4) $5 \times 10^{3}$

## Answer (2)

Sol. For 0.2 M solution
$R=50 \Omega$
$\sigma=1.4 \mathrm{~S} \mathrm{~m}^{-1}=1.4 \times 10^{-2} \mathrm{~S} \mathrm{~cm}^{-1}$
$\Rightarrow \rho=\frac{1}{\sigma}=\frac{1}{1.4 \times 10^{-2}} \Omega \mathrm{~cm}$
Now, $R=\rho \frac{l}{\mathrm{a}}$
$\Rightarrow \frac{l}{\mathrm{a}}=\frac{\mathrm{R}}{\rho}=50 \times 1.4 \times 10^{-2}$
For 0.5 M solution
$\mathrm{R}=280 \Omega$
$\sigma=$ ?
$\frac{l}{a}=50 \times 1.4 \times 10^{-2}$
$\Rightarrow \mathrm{R}=\rho \frac{l}{\mathrm{a}}$
$\Rightarrow \frac{1}{\rho}=\frac{1}{R} \times \frac{l}{a}$
$\Rightarrow \sigma=\frac{1}{280} \times 50 \times 1.4 \times 10^{-2}$

$$
\begin{aligned}
& =\frac{1}{280} \times 70 \times 10^{-2} \\
& =2.5 \times 10^{-3} \mathrm{~S} \mathrm{~cm}^{-1}
\end{aligned}
$$

Now, $\lambda_{\mathrm{m}}=\frac{\sigma \times 1000}{\mathrm{M}}$

$$
\begin{aligned}
& =\frac{2.5 \times 10^{-3} \times 1000}{0.5} \\
& =5 \mathrm{~S} \mathrm{~cm}^{2} \mathrm{~mol}^{-1} \\
& =5 \times 10^{-4} \mathrm{~S} \mathrm{~m}^{2} \mathrm{~mol}^{-1}
\end{aligned}
$$

86. Among the following oxoacids, the correct decreasing order of acid strength is
(1) $\mathrm{HClO}_{2}>\mathrm{HClO}_{4}>\mathrm{HClO}_{3}>\mathrm{HOCl}$
(2) $\mathrm{HOCl}>\mathrm{HClO}_{2}>\mathrm{HClO}_{3}>\mathrm{HClO}_{4}$
(3) $\mathrm{HClO}_{4}>\mathrm{HOCl}>\mathrm{HClO}_{2}>\mathrm{HClO}_{3}$
(4) $\mathrm{HClO}_{4}>\mathrm{HClO}_{3}>\mathrm{HClO}_{2}>\mathrm{HOCl}$

Answer (4)

Sol. $\mathrm{HClO}_{4} \rightleftharpoons \mathrm{ClO}_{4}^{-}+\mathrm{H}^{+}$
$\mathrm{HClO}_{3} \rightleftharpoons \mathrm{ClO}_{3}^{-}+\mathrm{H}^{+}$
$\mathrm{HClO}_{2} \rightleftharpoons \mathrm{ClO}_{2}^{-}+\mathrm{H}^{+}$
$\mathrm{HOCl} \rightleftharpoons \mathrm{ClO}^{-}+\mathrm{H}^{+}$
Resonance produced conjugate base.
(i)


(ii)

(iii)

(iv) $\mathrm{ClO}^{-}$is not resonance stabilized.

As per resonance stability order of conjugate base is
$\mathrm{ClO}_{4}^{-}>\mathrm{ClO}_{3}^{-}>\mathrm{ClO}_{2}^{-}>\mathrm{ClO}^{-}$
Hence acidic strength order is
$\mathrm{HClO}_{4}>\mathrm{HClO}_{3}>\mathrm{HClO}_{2}>\mathrm{HClO}$
87. Which one of the following bases is not present in DNA?
(1) Thymine
(2) Quinoline
(3) Adenine
(4) Cytosine

## Answer (2)

Sol. DNA contains ATGC bases
A - Adenine
T - Thymine
G - Guanine
C - Cytocine
So quinoline is not present.
88. Considering the basic strength of amines in aqueous solution, which one has the smallest $\mathrm{pK}_{\mathrm{b}}$ value?
(1) $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{NH}_{2}$
(2) $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{NH}$
(3) $\mathrm{CH}_{3} \mathrm{NH}_{2}$
(4) $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{~N}$

## Answer (2)

Sol. Among $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{NH}_{2}, \mathrm{CH}_{3} \mathrm{NH}_{2},\left(\mathrm{CH}_{3}\right)_{2} \mathrm{NH}$,
$\left(\mathrm{CH}_{3}\right)_{3} \mathrm{~N} \cdot \mathrm{C}_{6} \mathrm{H}_{5} \mathrm{NH}_{2}$ is least basic due to resonance.


Out of $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{~N}, \mathrm{CH}_{3} \mathrm{NH}_{2},\left(\mathrm{CH}_{3}\right)_{2} \mathrm{NH} .\left(\mathrm{CH}_{3}\right)_{2} \mathrm{NH}$ is most basic due to +1 effect and hydrogen bonding in $\mathrm{H}_{2} \mathrm{O}$.

89. If Z is a compressibility factor, van der Waals equation at low pressure can be written as
(1) $\mathrm{Z}=1+\frac{\mathrm{Pb}}{\mathrm{RT}}$
(2) $\mathrm{Z}=1+\frac{\mathrm{RT}}{\mathrm{Pb}}$
(3) $\mathrm{Z}=1-\frac{\mathrm{a}}{\mathrm{VRT}}$
(4) $\mathrm{Z}=1-\frac{\mathrm{Pb}}{\mathrm{RT}}$

## Answer (3)

Sol. Compressibility factor $(Z)=\frac{P V}{R T}$
(For one mole of real gas)
van der Waal equation
$\left(\mathrm{P}+\frac{\mathrm{a}}{\mathrm{V}^{2}}\right)(\mathrm{V}-\mathrm{b})=\mathrm{RT}$
At low pressure
$\mathrm{V}-\mathrm{b} \approx \mathrm{V}$
$\left(\mathrm{P}+\frac{\mathrm{a}}{\mathrm{V}^{2}}\right) \mathrm{V}=\mathrm{RT}$
$\mathrm{PV}+\frac{\mathrm{a}}{\mathrm{V}}=\mathrm{RT}$
$P V=R T-\frac{a}{V}$
$\frac{\mathrm{PV}}{\mathrm{RT}}=1-\frac{\mathrm{a}}{\mathrm{VRT}}$
So, $Z=1-\frac{\mathrm{a}}{\mathrm{VRT}}$
90. Which series of reactions correctly represents chemical reactions related to iron and its compound?
(1) $\mathrm{Fe} \xrightarrow{\mathrm{O}_{2} \text {, heat }} \mathrm{Fe}_{3} \mathrm{O}_{4} \xrightarrow{\mathrm{CO}, 600^{\circ} \mathrm{C}}$
$\mathrm{FeO} \xrightarrow{\mathrm{CO}, 700^{\circ} \mathrm{C}} \mathrm{Fe}$
(2) $\mathrm{Fe} \xrightarrow{\text { dil. } \mathrm{H}_{2} \mathrm{SO}_{4}} \mathrm{FeSO}_{4} \xrightarrow{\mathrm{H}_{2} \mathrm{SO}_{4}, \mathrm{O}_{2}}$ $\mathrm{Fe}_{2}\left(\mathrm{SO}_{4}\right)_{3} \xrightarrow{\text { heat }} \mathrm{Fe}$
(3) $\mathrm{Fe} \xrightarrow{\mathrm{O}_{2} \text {, heat }} \mathrm{FeO} \xrightarrow{\text { dil. } \mathrm{H}_{2} \mathrm{SO}_{4}}$ $\mathrm{FeSO}_{4} \xrightarrow{\text { heat }} \mathrm{Fe}$
(4) $\mathrm{Fe} \xrightarrow{\mathrm{Cl}_{2}, \text { heat }} \mathrm{FeCl}_{3} \xrightarrow{\text { heat, air }}$ $\mathrm{FeCl}_{2} \xrightarrow{\mathrm{Zn}} \mathrm{Fe}$
Answer (4)
Sol. Anhydrous ferric chloride is prepared by passing dry chlorine gas over heated iron fillings.
$2 \mathrm{Fe}+3 \mathrm{Cl}_{2} \longrightarrow 2 \mathrm{FeCl}_{3}$
$\mathrm{FeCl}_{3}$ on heating gives $\mathrm{FeCl}_{2}$ and $\mathrm{Cl}_{2}$
$\mathrm{FeCl}_{3} \xrightarrow{\Delta} 2 \mathrm{FeCl}_{2}+\mathrm{Cl}_{2}$
$\mathrm{FeCl}_{3}$ is reduced by Zn form Fe and $\mathrm{ZnCl}_{2}$
$\mathrm{FeCl}_{2}+\mathrm{Zn} \longrightarrow \mathrm{Fe}+\mathrm{ZnCl}_{2}$


[^0]:    1,1,1-trichloroethane

