## AIPMT - 2014 TEST PAPER WITH SOLUTIONS (HELD ON SUNDAY 04 ${ }^{\text {th }}$ MAY, 2014)

1. If force ( F ), velocity $(\mathrm{V})$ and time $(\mathrm{T})$ are taken as fundamental units, then the dimensions of mass are:-
(1) $\left[\mathrm{F} \mathrm{V} \mathrm{T}^{-1}\right]$
(2) $\left[\mathrm{F} \mathrm{V} \mathrm{T}^{-2}\right]$
(3) $\left[\mathrm{F} \mathrm{V}^{-1} \mathrm{~T}^{-1}\right]$
(4) $\left[\mathrm{F} \mathrm{V}^{-1} \mathrm{~T}\right]$

Ans. (4)
Sol. $\quad[$ mass $]=\left[\frac{\text { Force }}{\text { Acceleration }}\right]=\left[\frac{\text { Force }}{\text { Velocity } / \text { time }}\right]$

$$
=\left[\mathrm{F} \mathrm{~V}^{-1} \mathrm{~T}\right]
$$

2 A projectile is fired from the surface of the earth with a velocity of $5 \mathrm{~ms}^{-1}$ and angle $\theta$ with the horizontal. Another projectile fired from another planet with a velocity of $3 \mathrm{~ms}^{-1}$ at the same angle follows a trajectory which is identical with the trajectory of the projectile fired fromthe earth. The value of the acceleration dueto gravity on the planet is (in ms ${ }^{-2}$ ) given $\mathrm{g}=9.8 \mathrm{~m} / \mathrm{s}^{2}$
(1) 3.5
(2) 5.9
(3) 16.3
(4) 110.8

Ans. (1)
Sol. As Range $=\frac{\mathrm{u}^{2} \sin 2 \theta}{\mathrm{~g}}$ so $\mathrm{g} \propto \mathrm{u}^{2}$

Therefore $g_{\text {planet }}=\left(\frac{3}{5}\right)^{2}\left(9.8 \mathrm{~m} / \mathrm{s} q=3.5 \mathrm{~m} / \mathrm{s}^{2}\right.$
3. A particle is moving such that its position coordinate ( $\mathrm{x}, \mathrm{y}$ ) are
$(2 \mathrm{~m}, 3 \mathrm{~m})$ at time $\mathrm{t}=0$
$(6 \mathrm{~m}, 7 \mathrm{~m})$ at time $\mathrm{t}=2 \mathrm{~s}$ and
$(13 \mathrm{~m}, 14 \mathrm{~m})$ at time $\mathrm{t}=5 \mathrm{~s}$.
Average velocity vector ( $\overrightarrow{\mathrm{V}}_{\mathrm{av}}$ ) from $\mathrm{t}=0$ to $\mathrm{t}=5$ $s$ is :-
(1) $\frac{1}{5}(13 \hat{i}+14 \hat{j})$
(2) $\frac{7}{3}(\hat{\mathrm{i}}+\hat{\mathrm{j}})$
(3) $2(\hat{i}+\hat{\mathrm{j}})$
(4) $\frac{11}{5}(\hat{i}+\hat{j})$

## Ans. (4)

Sol. $\quad \overrightarrow{\mathrm{v}}_{\mathrm{av}}=\frac{\Delta \overrightarrow{\mathrm{r}}}{\Delta \mathrm{t}}=\frac{(13-2) \hat{\mathrm{i}}+(14-3) \hat{\mathrm{j}}}{5-0}=\frac{11}{5}(\hat{\mathrm{i}}+\hat{\mathrm{j}})$
4. A system consists of three masses $m \quad 1, m_{2}$ and $m_{3}$ connected by a string passing over a pulley P . The mass $\mathrm{m}_{1}$ hangs freely and $\mathrm{m}_{2}$ and $\mathrm{m}_{3}$ are onarough horizontal table (the coefficient of friction $=\mu$ ). The pulley is frictionless and of negligible mass. The downward acceleration of mass $\mathrm{m}_{1}$ is :
(Assume $\mathrm{m}_{1}=\mathrm{m}_{2}=\mathrm{m}_{3}=\mathrm{m}$ )

(1) $\frac{g(1-g \mu)}{9}$
(2) $\frac{2 g \mu}{3}$
(3) $\frac{\mathrm{g}(1-2 \mu)}{3}$
(4) $\frac{\mathrm{g}(1-2 \mu)}{2}$

Ans. (3)
Sol. $\quad$ Acceleration $=\frac{\text { Net force in the direction of motion }}{\text { Total mass of system }}$

$$
=\frac{m_{1} g-\mu\left(m_{2}+m_{3}\right) g}{m_{1}+m_{2}+m_{3}}=\frac{g}{3}(1-2 \mu)
$$

5. The force ' $F$ ' acting on a particle of mass ' $m$ ' is indicated by the force-time graph shownbelow. The change in momentum of the particle over the time interval from zero to 8 s is :-

(1) 24 Ns
(2) 20 Ns
(3) 12 Ns
(4) 6 Ns

Ans. (3)
Sol. Change in momentum,

$$
\begin{aligned}
\Delta \mathrm{p} & =\int \text { Fdt } \\
& =\text { Area of F-t graph } \\
& =\frac{1}{2} \times 2 \times 6-3 \times 2+4 \times 3 \\
& =12 \mathrm{~N}-\mathrm{s}
\end{aligned}
$$

6. A balloon with mass ' $m$ ' is descending down with an acceleration 'a' (where $\mathrm{a}<\mathrm{g}$ ). How much mass should be removed from it so that it starts moving up with an acceleration 'a' ?
(1) $\frac{2 m a}{g+a}$
(2) $\frac{2 m a}{g-a}$
(3) $\frac{m a}{g+a}$
(4) $\frac{m a}{g-a}$

Ans. (1)
Sol. Let upthrust of air be F a then for downward motion
$m g-F_{a}=m a$
for upward motion
$F_{a}-(m-\Delta m)=(m-\Delta m) a$
Therefore $\Delta \mathrm{m}=\frac{2 \mathrm{ma}}{\mathrm{g}+\mathrm{a}}$
7. A body of mass $(4 \mathrm{~m})$ is lying in $x-y$ plane at rest. It suddenly explodes into three pieces. Two pieces, each of mass ( m ) move perpendicular to each other with equal speeds (v). The total kinetic energy generated due to explosion is :-
(1) $\mathrm{mv}^{2}$
(2) $\frac{3}{2} \mathrm{mv}^{2}$
(3) $2 \mathrm{mv}^{2}$
(4) $4 \mathrm{mv}^{2}$

Ans. (2)

Sol.


By conservation of linear momentum

$$
2 m v_{1}=\sqrt{2} \mathrm{mv} \Rightarrow \mathrm{v}_{1}=\frac{\mathrm{v}}{\sqrt{2}}
$$

Total KE generated $=\frac{1}{2} \mathrm{mv}^{2}+\frac{1}{2} \mathrm{mv}^{2}+\frac{1}{2}(2 \mathrm{~m}) \mathrm{v}_{1}^{2}$

$$
=m v^{2}+\frac{m v^{2}}{2}=\frac{3}{2} m v^{2}
$$

8. The oscillation of a body on a smooth horizontal surface is represented by the equation,

$$
\mathrm{X}=\mathrm{A} \cos (\omega \mathrm{t})
$$

where $\quad \mathrm{X}=$ displacement at time t

$$
\omega=\text { frequency of oscillation }
$$

Which one of the following graphs shows correctly the variation 'a' with 't' ?
(1)

(2)

(3)

(4)


Ans. (3)
Sol. Displacement, $\mathrm{x}=\mathrm{A} \cos (\omega \mathrm{t})$
Velocity, $\mathrm{v}=\frac{\mathrm{dx}}{\mathrm{dt}}=-\mathrm{A} \omega \sin (\omega \mathrm{t})$

Acceleration, $\mathrm{a}=\frac{\mathrm{d} v}{\mathrm{dt}}=-\mathrm{A} \omega^{2} \cos (\omega \mathrm{t})$
9. A solid cylinder of mass 50 kg and radius 0.5 m is free to rotate about the horizontal axis. A massless string is wound round the cylinder with one end attached to it and other hanging freely. Tension in the string required to produce an angular acceleration of 2 revolutions s -2 is :-
(1) 25 N
(2) 50 N
(3) 78.5 N
(4) 157 N

Ans. (4)
Sol. Here $\alpha=2$ revolutions $/ \mathrm{s}^{2}=4 \pi \mathrm{rad} / \mathrm{s}^{2}$
$I=\frac{1}{2} M R^{2}=\frac{1}{2}(50)(0.5)^{2}=\frac{25}{4} K g-m^{2}$
As $\tau=\mathrm{I} \alpha$ so $\mathrm{TR}=\mathrm{I} \alpha$
$\Rightarrow \mathrm{T}=\frac{\mathrm{I} \alpha}{\mathrm{R}}=\frac{\left(\frac{25}{4}\right)(4 \pi)}{(0.5)} \mathrm{N}=50 \quad \pi \mathrm{~N}=157 \mathrm{~N}$
10. The ratio of the accelerations for a soldi sphere (mass ' m ' and radius ' R ') rolling down an incline of angle ' $\theta$ ' without slipping and slipping down the incline without rolling is :-
(1) $5: 7$
(2) $2: 3$
(3) $2: 5$
(4) $7: 5$

Ans. (1)
Sol. For rolling motion without slipping on inclined plane

$$
\mathrm{a}_{1}=\frac{g \sin \theta}{1+\frac{\mathrm{K}^{2}}{\mathrm{R}^{2}}}
$$

and for slipping motion on inclined plane

$$
\mathrm{a}_{2}=\mathrm{g} \sin \theta
$$

Required ratio $=\frac{\mathrm{a}_{1}}{\mathrm{a}_{2}}=\frac{1}{1+\frac{\mathrm{K}^{2}}{\mathrm{R}^{2}}}=\frac{1}{1+\frac{2}{5}}=\frac{5}{7}$
11. A black hole is an object whose gravitational field is so strong that even light cannot escape from it. To what approximate radius would earth (mass = $5.98 \times 10{ }^{24} \mathrm{~kg}$ ) have to be compressed to be a black hole?
(1) $10^{-9} \mathrm{~m}$
(2) $10^{-6} \mathrm{~m}$
(3) $10^{-2} \mathrm{~m}$
(4) 100 m

Ans. (3)
Sol. Escape velocity $=\sqrt{\frac{2 \mathrm{GM}}{\mathrm{R}}}=\mathrm{c}=$ speed of light

$$
\begin{aligned}
\Rightarrow & \mathrm{R}
\end{aligned}=\frac{2 \mathrm{GM}}{\mathrm{c}^{2}}=\frac{2 \times 6.6 \times 10^{-11} 5.98 \quad 10{ }^{24}}{\left(3 \times 10^{8}\right)^{2}} \mathrm{~m}
$$

12. Dependence of intensity of gravitational field(E) of earth with distance (r) from centre of earth is correctly represented by :-
(1)

(2)

(3)

(4)


Ans. (1)
13. Copper of fixed volume ' V ; is drawn into wire of length' $I$. When this wire is subjected to a constant force ' F ', the extension produced in the wire is' $\Delta I$. Which of the following graphs is a straight line?
(1) $\Delta /$ versus $\frac{1}{l}$
(2) $\Delta l$ versus $R$
(3) $\Delta l$ versus $\frac{1}{R^{2}}$
(4) $\Delta /$ versus $I$

Ans. (2)

Sol. $Y=\frac{\frac{F}{A}}{\frac{\Delta \ell}{\ell}} \Rightarrow \Delta \ell=\frac{F \ell}{\mathrm{AY}}$

But $\mathrm{V}=\mathrm{A} \ell$ so $\mathrm{A}=\frac{\mathrm{V}}{\ell}$
Therefore $\Delta \ell=\frac{\mathrm{F} \ell^{2}}{\mathrm{VY}} \propto \ell^{2}$
14. A certain number of sphereical drops of a liquid of radius 'r' coalesce to form a single drop of radius ' R ' and volume ' V '. If ' T ' is the surface tension of the liquid, then :
(1) energy $=4 \mathrm{VT}\left(\frac{1}{\mathrm{r}}-\frac{1}{\mathrm{R}}\right)$ is released
(2) energy $=3 V T\left(\frac{1}{r}+\frac{1}{R}\right)$ is absorbed
(3) energy $=3 \mathrm{VT}\left(\frac{1}{\mathrm{r}}-\frac{1}{\mathrm{R}}\right)$ is released
(4) Energy is neither released nor absorbed

Ans. (3)
Sol. As surface area decreases so energy is released.
Released energy

$$
\begin{aligned}
& =4 \pi \mathrm{R}^{2} \mathrm{~T}\left[\mathrm{n}^{1 / 3}-1\right] \quad \text { where } \mathrm{R}=\mathrm{n}^{1 / 3} \mathrm{r} \\
& =4 \pi \mathrm{R}^{3} \mathrm{~T}\left[\frac{1}{\mathrm{r}}-\frac{1}{\mathrm{R}}\right] \\
& =3 \mathrm{VT}\left[\frac{1}{\mathrm{r}}-\frac{1}{\mathrm{R}}\right]
\end{aligned}
$$

15. Steam at $100^{\circ} \mathrm{C}$ is passed into 20 g of water at $10^{\circ} \mathrm{C}$. When water acquires a temperature of $80^{\circ} \mathrm{C}$, the mass of water present will be :
[Take specific heat of water $=1 \mathrm{cal} \mathrm{g} \quad-1{ }^{\circ} \mathrm{C}^{-1}$ and latent heat of steam $=540 \mathrm{cal} \mathrm{g} \quad-1$ ]
(1) 24 g
(2) 31.5 g
(3) 42.5 g
(4) 22.5 g

Ans. (4)
Sol. Heat lost $=$ Heat gained
$\mathrm{mLv}+\mathrm{ms}_{\mathrm{w}} \Delta \theta=\mathrm{m}_{\mathrm{W}} \mathrm{s}_{\mathrm{w}} \Delta \theta$
$\Rightarrow \mathrm{m} \times 540+\mathrm{m} \times 1 \times(100-80)$ $=20 \times 1 \times(80-10)$
$\Rightarrow \mathrm{m}=2.5 \mathrm{~g}$
Total mass of water $=(20+2.5) \mathrm{g}=22.5 \mathrm{~g}$
16. Certain quantity of water cools from $70^{\circ} \mathrm{C}$ to $60^{\circ} \mathrm{C}$ in the first 5 minutes and to $54^{\circ} \mathrm{C}$ in the next 5 minutes. The temperature of the surroundings is:-
(1) $45^{\circ} \mathrm{C}$
(2) $20^{\circ} \mathrm{C}$
(3) $42^{\circ} \mathrm{C}$
(4) $10^{\circ} \mathrm{C}$

Ans. (1)
Sol. By Newton's law of colling

$$
\begin{align*}
& \frac{\theta_{1}-\theta_{2}}{\mathrm{t}}=\mathrm{k}\left[\frac{\theta_{1}+\theta_{2}}{2}-\theta_{0}\right] \\
& \Rightarrow \frac{70-60}{5}=\mathrm{k}\left[\frac{70-60}{2}-\theta_{0}\right] \\
& \Rightarrow 2=\mathrm{k}\left[65-\theta_{0}\right] \ldots \ldots \ldots .(\mathrm{i})  \tag{i}\\
& \text { and } \frac{60-54}{5}=\mathrm{k}\left[\frac{\left.60 \frac{54}{2}-\theta_{0}\right]}{\Rightarrow} \frac{\frac{6}{5}=\mathrm{k}\left[57-\theta_{0}\right] \ldots . . . \text { (ii) }}{\Rightarrow}\right.
\end{align*}
$$

By dividing (i) by (ii) we have

$$
\frac{10}{5}=\frac{65-\theta_{0}}{37-\theta_{0}} \quad \Rightarrow \theta_{0}=45^{\circ}
$$

17. A monoatomic gas at a pressure P , having avolume V expands isothermally to a volume 2 V and then adibatically to a volume 16 V . The final pressure of the gas is: (take $\gamma=\frac{5}{3}$ )
(1) 64 P
(2) 32 P
(3) $\frac{P}{64}$
(4) 16 P

Ans. (3)

Sol. For isothermal process $\mathrm{P}_{1} \mathrm{~V}_{1}=\mathrm{P}_{2} \mathrm{~V}_{2}$
$\Rightarrow \mathrm{PV}=\mathrm{P}_{2}(2 \mathrm{~V}) \Rightarrow \mathrm{P}_{2}=\frac{\mathrm{P}}{2}$
For adiabatic process $\quad \mathrm{P}_{2} \mathrm{~V}_{2}^{\gamma}=\mathrm{P}_{3} \mathrm{~V}_{3}^{\gamma}$
$\Rightarrow\left(\frac{\mathrm{P}}{2}\right)(2 \mathrm{v})^{\gamma}=\mathrm{P}_{3}(16 \mathrm{v})^{\gamma}$
$\Rightarrow P_{3}=\frac{3}{2}\left(\frac{1}{8}\right)^{5 / 3}=\frac{P}{64}$
18. A thermodynamic systemundergoes cyclic process ABCDA as shown in fig. The work done by the system in the cycle is :-

(1) $P_{0} V_{0}$
(2) $2 \mathrm{P}_{0} \mathrm{~V}_{0}$
(3) $\frac{P_{0} V_{0}}{2}$
(4) Zero

Ans. (4)
Sol. Work done by the system in the cycle

$$
\begin{aligned}
& =\text { Area under } \mathrm{P}-\mathrm{V} \text { curve } \& \mathrm{~V} \text {-axis } \\
& =\frac{1}{2}\left(2 \mathrm{P}_{0}-\mathrm{P}_{0}\right)\left(2 \mathrm{~V}_{0}-\mathrm{V}_{0}\right)+ \\
& \quad\left[-\left(\frac{1}{2}\right)\left(3 \mathrm{P}_{0}-2 \mathrm{P}_{0}\right)\left(2 \mathrm{~V}_{0}-\mathrm{V}_{0}\right)\right] \\
& =\frac{\mathrm{P}_{0} \mathrm{~V}_{0}}{2}-\frac{\mathrm{P}_{0} \mathrm{~V}_{0}}{2}=0
\end{aligned}
$$

19. The mean free path of molecules of a gas, (radius ' $r$ ') is inversely proportional to :-
(1) $r^{3}$
(2) $r^{2}$
(3) $r$
(4) $\sqrt{r}$

Ans. (2)
Sol. Mean free path $\quad \lambda_{\mathrm{m}}=\frac{1}{\sqrt{2} \pi \mathrm{~d}^{2} \mathrm{n}}$
where $\mathrm{d}=$ diameter of molecule
$\Rightarrow \lambda_{\mathrm{m}} \propto \frac{1}{\mathrm{r}^{2}}$
20. If $\mathrm{n}_{1}, \mathrm{n}_{2}$ and $\mathrm{n}_{3}$ are the fundamental frequencies of three segments into which a string is divided, then the original fundamental frequency $n$ of the string is given by :-
(1) $\frac{1}{\mathrm{n}}=\frac{1}{\mathrm{n}_{1}}+\frac{1}{\mathrm{n}_{2}}+\frac{1}{\mathrm{n}_{3}}$
(2) $\frac{1}{\sqrt{\mathrm{n}}}=\frac{1}{\sqrt{\mathrm{n}_{1}}}+\frac{1}{\sqrt{\mathrm{n}_{2}}}+\frac{1}{\sqrt{\mathrm{n}_{3}}}$
(3) $\sqrt{\mathrm{n}}=\sqrt{\mathrm{n}_{1}}+\sqrt{\mathrm{n}_{2}}+\sqrt{\mathrm{n}_{3}}$
(3) $n=n_{1}+n_{2}+n_{3}$

Ans. (1)
Sol. Total length of string $\ell=\ell_{1}+\ell_{2}+\ell_{3}$
But frequency $\propto \frac{1}{\text { length }}$
so $\frac{1}{\mathrm{n}}=\frac{1}{\mathrm{n}_{1}}+\frac{1}{\mathrm{n}_{2}}+\frac{1}{\mathrm{n}_{3}}$
21. The number of possible natural oscillation of air column in a pipe closed at one end of length 85 cm whose frequencies lie below 1250 Hz are : (velocity of sound $=340 \mathrm{~ms}^{-1}$ )
(1) 4
(2) 5
(3) 7
(4) 6

Ans. (4)
Sol. Frequency COP, $f_{n}=(2 n+1) \frac{v}{4 R}$
for $\mathrm{n}=0, \quad \mathrm{f}_{0}=100 \mathrm{~Hz}$

$$
\begin{array}{ll}
\mathrm{n}=1, & \mathrm{f}_{1}=300 \mathrm{~Hz} \\
\mathrm{n}=2, & \mathrm{f}_{2}=500 \mathrm{~Hz} \\
\mathrm{n}=3, & \mathrm{f}_{3}=700 \mathrm{~Hz} \\
\mathrm{n}=4, & \mathrm{f}_{4}=900 \mathrm{~Hz} \\
\mathrm{n}=5, & \mathrm{f}_{5}=1100 \mathrm{~Hz}
\end{array}
$$

Which are less than 1250 Hz .
22. A speeding motorcyclist sees trafic jam ahead of him. He slows down to 36 km hour. He finds that traffic has eased and a car moving ahead of him at 18 km hour is honking at a frequency of 1392 Hz . If the speeds of sound is $343 \mathrm{~m} /$, the frequency of the honk as heard by him will be :-
(1) 1332 Hz
(2) 1372 Hz
(3) 1412 Hz
(4) 1464 Hz

Ans. (3)
Sol. Apparent frequency

$$
\mathrm{n}^{\prime}=\mathrm{n}\left(\frac{\mathrm{v}+\mathrm{v}_{0}}{\mathrm{v}+\mathrm{v}_{3}}\right)=1392\left(\frac{343+10}{343+5}\right)=1412 \mathrm{~Hz}
$$

23. Two thin dielectric slabs of dielectric constants $\mathrm{K} \quad 1$ and $\mathrm{K}_{2}\left(\mathrm{~K}_{1}<\mathrm{K}_{2}\right)$ are inserted between plates of a parallel plate capacitor, as shown in the figure. The variation of electric field 'E' between the plates with distance ' d ' as measured from plate P is correctly shown by :-

(1)

(2)

(3)

(4)


Ans. (3)
Sol. Electric field, $\mathrm{E} \propto \frac{1}{\mathrm{~K}}$
As $K_{1}<K_{2}$ so $E_{1}>E_{2}$
24. A conducting sphere of radius R is given a charge Q. The electric potential and the electric field at the centre of the sphere respectively are :-
(1) Zero and $\frac{\mathrm{Q}}{4 \pi \in_{0} \mathrm{R}^{2}}$
(2) $\frac{\mathrm{Q}}{4 \pi \in_{0} \mathrm{R}}$ and Zero
(3) $\frac{\mathrm{Q}}{4 \pi \epsilon_{0} \mathrm{R}}$ and $\frac{\mathrm{Q}}{4 \pi \epsilon_{0} \mathrm{R}^{2}}$
(4) Both are zero

Ans. (2)
Sol. At centre, $\mathrm{E}=0 \& \mathrm{~V}=\frac{\mathrm{Q}}{4 \pi \in_{0} \mathrm{R}}$
28. A potentiometer circuit has been set up for finding the internal resistance of a given cell. The main battery used across the potentiometer wire, has an emf of 2.0 V and a negligible internal resistance. The potentiometer wire itself is 4mlong, When the resistace R , connected across the given cell, has values of.
(i) infinity
(ii) $9.5 \Omega$

The balancing lengths', on the potentiometer wire are found to be 3 m and 2.85 m , respectively.
The value of internal resistance of the cell is
(1) $0.25 \Omega$
(2) $0.95 \Omega$
(3) $0.5 \Omega$
(4) $0.75 \Omega$

Ans. (3)
Sol. Internal resistance, $r=\left(\frac{E-V}{V}\right) R=\left(\frac{\ell_{1}-\ell_{2}}{\ell_{2}}\right) R$

$$
=\left(\frac{3-2.85}{2.85}\right)(9.5) \Omega=0.5 \Omega
$$

29. Following figures show the arrangement of bar magnets in different configurations. Each magnet has magnetic dipole moment $\overrightarrow{\mathrm{m}}$. Which configuration has highest net magnetic diple moment?
Ans. (2)
Sol. Resistance $=(0.5 \Omega / \mathrm{km})(150 \mathrm{~km})=75 \Omega$
Total voltage drop $=(8 \mathrm{~V} / \mathrm{km})(150 \mathrm{~km})=1200 \mathrm{~V}$

$$
\begin{aligned}
\text { Power loss } & =\frac{(\Delta \mathrm{V})^{2}}{\mathrm{R}}=\frac{(1200)^{2}}{75} \mathrm{~W} \\
& =19200 \mathrm{~W}=19.2 \mathrm{~kW}
\end{aligned}
$$

27. The resistance in the two arms of the meter bridge are $5 \Omega$ and $R \Omega$, respectively. When the resistance $R$ is shunted with an equal resistance, the new balance point is at $1.6 \quad \ell_{1}$. The resistance ' $R$ ' is :-

(1) $10 \Omega$
(2) $15 \Omega$
(3) $20 \Omega$
(4) $25 \Omega$

Ans. (2)
Sol. $\frac{5}{\mathrm{R}}=\frac{\ell_{1}}{100-\ell_{1}}$ and $\frac{5}{\mathrm{R} / 2}=\frac{1.6 \ell_{1}}{1004.6 \ell_{1}}$
$\Rightarrow \mathrm{R}=15 \Omega$
(a)

(b)

(c)

(d)

(1) (a)
(2) (b)
(3) (c)
(4) (d)

Ans. (3)
Sol. Net magnetic moment $=2 \operatorname{Mcos} \frac{\theta}{2}$
which is maximumfor option (3)
30. In an ammeter $0.2 \%$ of main current passes through the galvanometer. If resistance of galvanometer is G , the resistance of ammeter will be :-
(1) $\frac{1}{499} G$
(2) $\frac{499}{500} \mathrm{G}$
(3) $\frac{1}{500} \mathrm{G}$
(4) $\frac{500}{499} \mathrm{G}$

Ans. (3)

Sol.

$\left(\frac{2 \mathrm{I}}{1000}\right) \mathrm{G}=\left(\frac{998 \mathrm{I}}{1000}\right) \mathrm{S}$
$\Rightarrow \mathrm{S}=\frac{\mathrm{G}}{499}$
Total resistance of Ammeter
$R=\frac{S G}{S+G}=\frac{\left(\frac{G}{499}\right) F}{\left(\frac{G}{499}\right)+G}=\frac{G}{500}$
31. Two identical long conducting wires $A O B$ and $C O D$ are placed at right angle to each other, with one above other such that ' $O$ ' is their common point for the two. The wires carry I $1_{1}$ and $\mathrm{I}_{2}$ currents respectively. Point ' $P$ ' is lying at distance ' $d$ ' from ' O ' along a direction perpendicular to the plane containing the wires. The magnetic field at the point ' $P$ ' will be :-
(1) $\frac{\mu_{0}}{2 \pi \mathrm{~d}}\left(\mathrm{I}_{1} / \mathrm{I}_{2}\right)$
(2) $\frac{\mu_{0}}{2 \pi \mathrm{~d}}\left(\mathrm{I}_{1}+\frac{\mathrm{L}}{}\right)$
(3) $\frac{\mu_{0}}{2 \pi d}\left(l_{1}^{2}-\frac{p}{2}\right)$
(4) $\frac{\mu_{0}}{2 \pi \mathrm{~d}}\left(l_{1}^{2}+\tilde{R}_{2}^{2}\right)^{2}$

Ans. (4)
Sol. Net magnetic field, $\mathrm{B}=\sqrt{\mathrm{B}_{1}^{2}+\mathrm{B}_{2}^{2}}$

$$
\begin{aligned}
& =\sqrt{\left(\frac{\mu_{0} I_{1}}{2 \pi \mathrm{~d}}\right)^{2}+\left(\frac{\mu_{0} \underline{b}}{2 \pi \mathrm{~d}}\right)^{2}} \\
& =\frac{\mu_{0}}{2 \pi \mathrm{~d}} \sqrt{\mathrm{I}_{1}^{2}+\mathrm{I}_{2}^{2}}
\end{aligned}
$$

32. A thin semicircular conducting ring ( PQR ) of radius ' $r$ ' is falling with its plane vertical in a horizontal magnetic field $B$, as shown in figure. The potential difference developed across the ring whenits speed is $v$, is :-

(1) Zero
(2) $\mathrm{Bv} \pi \mathrm{r}^{2} / 2$ and P is at higher potnetial
(3) $\pi \mathrm{rBv}$ and R is at higher potnetial
(4) $2 r B v$ and $R$ is at higher potential

Ans. (4)

Sol.


Induced emf $=\operatorname{Bv}(2 r)=2 r B v$
33. A transformer having efficiency of $90 \%$ is working on 200 V and 3 kW power supply. If the current in the secondary coil is 6 A , the voltage across the secondary coil and the current in the primary coil respectively are :-
(1) $300 \mathrm{~V}, 15 \mathrm{~A}$
(2) $450 \mathrm{~V}, 15 \mathrm{~A}$
(3) $450 \mathrm{~V}, 13.5 \mathrm{~A}$
(4) $600 \mathrm{~V}, 15 \mathrm{~A}$

Ans. (2)
Sol. $\quad \eta=\frac{V_{S} I_{S}}{V_{P} I_{P}} \Rightarrow 0.9=\frac{V_{S}(6)}{3 \times 10^{3}} \Rightarrow V_{S}=450 \mathrm{~V}$

As $V_{P} I_{P}=3000$ so I $P=\frac{3000}{200} \mathrm{~A}=15 \mathrm{~A}$
34. Light with an energy flux of $25 \times 10 \quad{ }^{4} \mathrm{Wm}^{-2}$ falls on a perfectly reflecting surface at normal incidence.
If the surface area is $15 \mathrm{~cm}^{2}$, the average force exerted on the surface is :-
(1) $1.25 \times 10-6 \mathrm{~N}$
(2) $2.50 \times 10-6 \mathrm{~N}$
(3) $1.20 \times 10-6 \mathrm{~N}$
(4) $3.0 \times 10-6 \mathrm{~N}$

Ans. (2)
Sol. Average force $\mathrm{F}_{\mathrm{av}}=\frac{\Delta \mathrm{p}}{\Delta \mathrm{t}}=\frac{2 \mathrm{IA}}{\mathrm{c}}$

$$
\begin{aligned}
& =\frac{2 \times 25 \times 10^{4} \not 15 * 0^{-4}}{3 \times 10^{8}} \\
& =2.50 \times 10^{-6} \mathrm{~N}
\end{aligned}
$$

35. A beam of light of $\lambda=600 \mathrm{~nm}$ fromadistant source falls on a single slit 1 mm wide and the resulting diffraction pattern is observed on a screen 2 m away. The distance between first dark fringes on either side of the central bright fringe is :-
(1) 1.2 cm
(2) 1.2 mm
(3) 2.4 cm
(4) 2.4 mm

Ans. (4)
Sol. Width of central bright fringe

$$
\begin{aligned}
& =\frac{2 \lambda \mathrm{D}}{\lambda}=\frac{2 \times 600 \times 10^{-6} \mathrm{z}}{1 \times 10^{-3}} \mathrm{~m} \\
& =2.4 \times 10^{-3} \mathrm{~m} \\
& =2.4 \mathrm{~mm}
\end{aligned}
$$

36. In the Young's double-slit experiment, the intensity of light at a point on the screen where the path difference is $\lambda$ is K , ( $\lambda$ being the wave length of light used). The intensity at a poijnt where the path difference is $\lambda / 4$, will be :-
(1) K
(2) $\mathrm{K} / 4$
(3) $K / 2$
(4) Zero

Ans. (3)
Sol. For path difference $\lambda$, phase difference $=2 \pi \mathrm{rad}$ For path difference $\frac{\lambda}{4}$, phase difference $=\frac{\pi}{2} \mathrm{rad}$
As $\mathrm{K}=4 \mathrm{I}_{0}$ so intensity at given point where path
difference is $\frac{\lambda}{4}$
$K^{\prime}=4 I_{0} \cos ^{2}\left(\frac{\pi}{4}\right)=2 I_{0}=\frac{K}{2}$
37. If the focal length of objective lens is increased then magnefying power of :-
(1) microscope will increase but that of telescope decrease.
(2) microscope and telescope both will increase.
(3) microscope and telescope both will decrease
(4) microscope will decrease but that of telescope increase.
Ans. (4)
Sol. Magnifying power of Microscope $=\frac{L D}{\mathrm{f}_{0} \mathrm{f}_{e}} \propto \frac{1}{f_{0}}$
Magnifying power of Telescope $=\frac{\mathrm{f}_{0}}{\mathrm{f}_{e}} \propto f_{0}$
38. The angle of a prism is ' A '. One of its refracting surfaces is silvered. Light rays falling at an angle of incidence 2 A on the first surface returns back through the same path after suffering reflection at the silvered surface. The refractive index $\mu$, of the prism is :-
(1) $2 \sin A$
(2) $2 \cos \mathrm{~A}$
(3) $\frac{1}{2} \cos \mathrm{~A}$
(4) $\tan A$

Ans. (2)

Sol.


By Snell's law
(1) $\sin 2 A=(\mu) \sin A \Rightarrow \mu=2 \cos A$
39. When the energy of the incident radiation is incredased by $20 \%$, the kinetic energy of the photoelectrons emitted from a metal surface increased from 0.5 eV to 0.8 eV . The work function of the metal is :-
(1) 0.65 eV
(2) 1.0 eV
(3) 1.3 eV
(4) 1.5 eV

Ans. (2)
Sol. By using $h v=\phi_{0}+K_{\text {max }}$
We have

$$
\begin{equation*}
h \nu=\phi_{0}+0.5 \tag{i}
\end{equation*}
$$

and $\quad 1.2 \mathrm{~h} v=\phi_{0}+0.8$
Therefore $\phi_{0}=1.0 \mathrm{eV}$
40. If the kinetic energy of the particle is increased to 16times its previous value, the percentage change in the de-Broglie wavelength of the particle is :-
(1) 25
(2) 75
(3) 60
(4) 50

Ans. (2)
Sol. $\quad l=\frac{h}{\sqrt{2 \mathrm{mK}}}$
$\frac{\lambda_{1}}{\lambda_{2}}=\sqrt{\frac{\mathrm{K}_{2}}{\mathrm{~K}_{1}}}=\sqrt{\frac{16 \mathrm{~K}}{\mathrm{~K}}}=\frac{4}{1}$
$=\frac{1-4}{4} \times 100=-75 \%$
41. Hydrogne atom is ground state is excited by a monochromatic radiation of $\lambda=975 \AA$. Number of spectral lines in the resulting spectrumemitted will be
(1) 3
(2) 2
(3) 6
(4) 10

Ans. (3)
42. The Binding energy per nucleon of ${ }_{3}^{7} \mathrm{Li}$ and ${ }_{2}^{4} \mathrm{He}$ nuclei are 5.60 MeV and 7.06 MeV , respectively.

In the nuclear reaction ${ }_{3}^{7} \mathrm{Li}+{ }_{1}^{1} \mathrm{H} \rightarrow{ }_{2}^{4} \mathrm{He}+\mathrm{Q}$, the value of energy $Q$ released is :-
(1) 19.6 MeV
(2) -2.4 MeV
(3) 8.4 MeV
(4) 17.3 MeV

Ans. (4)
Sol. $\quad \mathrm{BE}$ of ${ }_{2} \mathrm{He}^{4}=4 \times 7.06=28.24 \mathrm{MeV}$
BE of ${ }_{3} \mathrm{Li}=7 \times 5.60=39.20 \mathrm{MeV}$

$$
{ }_{3}^{7} \mathrm{Li}+{ }_{1}^{1} \mathrm{H} \longrightarrow{ }_{2} \mathrm{He}^{4}+{ }_{2} \mathrm{He}^{4}+\mathrm{Q}
$$

$$
39.20 \quad 28.24 \times 2
$$

$\mathrm{Q}=56.48-39.20=17.28 \mathrm{MeV}$
43. A radio isotope ' X ' with a half life $1.4 \times 10 \quad{ }^{9}$ years decays to ' Y ' which is stable. A sample of the rock from a cave was found to contain ' X ' and ' Y ' in the ratio $1: 7$. The age of the rock is :
(1) $1.96 \times 10{ }^{9}$ years
(2) $3.92 \times 10{ }^{9}$ years
(3) $4.20 \times 10{ }^{9}$ years
(4) $8.40 \times 10{ }^{9}$ years

Ans. (3)

Sol. As $\frac{\mathrm{N}_{\mathrm{x}}}{\mathrm{N}_{\mathrm{y}}}=\frac{1}{7} \Rightarrow \frac{\mathrm{~N}_{\mathrm{x}}}{\mathrm{N}_{\mathrm{x}}+\mathrm{N}_{\mathrm{y}}}=\frac{1}{8}=\left(\frac{1}{2}\right)^{3}$ sot $=3 \mathrm{~T}_{1 / 2}=3 \times 1.4 \times 10^{9}$ yrs. $=4.2 \times 10^{9} \mathrm{yrs}$.
44. The given graph represents V-I characteristic for a semiconductor device.


Which of the following statement is correct ?
(1) It is V-I characteristic for solar cell where, point A represents open circuit voltage and point $B$ short circuit current.
(2) It is a for a solar cell and point A and B represent open circuit voltage and current, respectively.
(3) It is for a photodiode and points A and B represent open circuit voltage and current, respectively.
(4) It is for a LED and points $A$ and $B$ represent open circuit voltage and short circuit current, respectively.
Ans. (1)
45. The barrier potential of ap-njunction depends on:
(a) type of semi conductor material
(g) amount of doping
(c) temperature

Which one of the following is correct ?
(1) (a) and (b) only
(2) (b) only
(3) (b) and (c ) only
(4) (a), (b) and (c)

Ans. (4)

